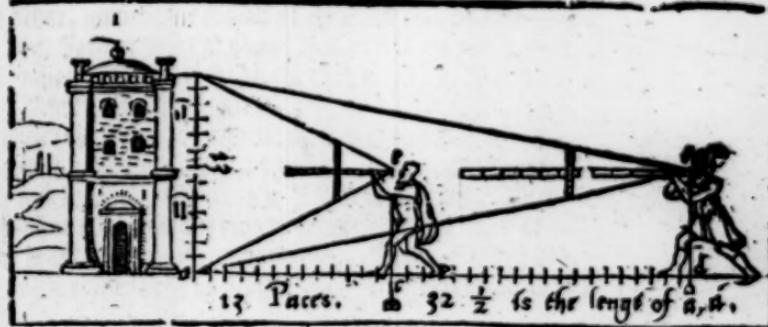


A  
2

# BOOKE NAMED TECTONICON,

Briefly shewing the exact Measuring, and speedie reckning all manner of Land, Squares, Timber, Stone, Steeples, Pillers, Globes, &c. Further, declaring the perfet making and large use of the Carpenters Rule, containing a Quadrane Geometrical: comprehending also the rare vse of the Squire. And in the end a little Treatise adioyning, opening the composition and appliance of an Instrument, called the profitable Staffe. With other things pleasant and necessary, most conduicible for Surveyors, Landmeaters, Joyners, Carpenters, and Masons.

Published by LEONARD DIGGES Gentleman, in  
the yeere of our Lord, 1556.  
*See Palmer book 1637.*



*AT LONDON*

Imprinted by Felix Kyngston, and are to be sold by Robert Allott, at the signe of the Grey-hound in Paules Church-yard. 1626.



142. *Journal d'un voyage au Levant* (1811).  
Par Adolphe de Joncières, membre de l'Institut, et de la Société des sciences  
naturelles de Paris, et de l'Académie de l'Institut de France, etc.  
Paris, chez l'auteur, 1811. In-8°, 12 volumes.

NOV 23 1971

and will be able to do so by the end of the year.

**D E S I G N**

How to measure all manner  
Triangled Land.

*The iij. Chapter.*

**I**f thou bee an Arithmetician, multiply this streight hanging line, byalwe, as above is shew-  
ed, in halfe the number of Peaches of that side,  
which it cutteth squirewise. For want of the  
knowledge, take the aforesnamed Peaches (A  
meane of the hanging line, and halfe the side which be cutteth)  
and with that length and breadth enter your Table of account,  
as there is set forth. So shall ye perceiue the number of Acres,  
Roodes, Dayworkes, &c.

Example.

**D**O the perfect measuring of Triangles afore figured, and  
all other, suppose the second of these last nine figures of the  
other side, having written about it a. b. c. d. to bee a piece of  
Land, whereof I would haue the true measure, I finde by a  
Cord, otherwise, the pricked hanging line a. b. to bee 23.  
Peaches: the side b. c. which it cutteth squirewise 44. Peaches:  
whose halfe is 22. With those 22. and 23. the conuenient  
length and breadth, I enter the Table of account. There I  
finde by that Table, at the corner where both the lines of con-  
uenient length and breadth doe meete, 3. Acres, 6. dayworks,  
and two Peaches to be in that Triangle. Thus of all before  
figured.

Here note your Table must ever bee entred with all the Peaches of the hanging line, and with halfe the side that bee cutteth squirewise. **D**o with the halfe hanging line, and the whole side cut.

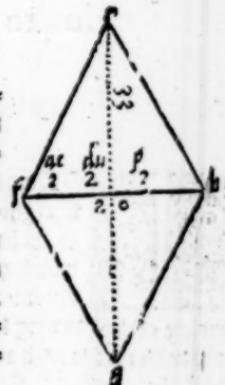
B

A

The Art of

A figure of a double  
Triangle.

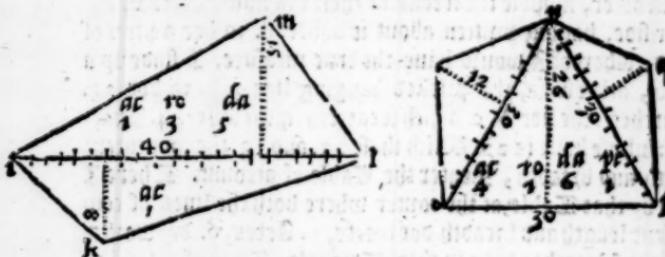
This figure c. f. g. h. is but two Triangles: and therefore measured as above in two parts. Or thus: The hanging line, e. g. is 33. Peartches: the side f. h. that he cutteth squarewise 20. Peartches, the halfe of the which is 10. Now enter your Table as afore, with 33. and 10. the convenient length and breadth. So shall ye finde two Acres, two Dayworks, and two Peartches, the true content of this figure c. f. g. h.



Another example.

Figures of ma-  
ny Angles.

Admit i. k. l. m. Land to bee measured. Because it is no manner Triangle, it must be brought by imagination, as I haue said, into a Triangle or Triangles. Which imaginatiōn is here signified by the line dashed i. l. Then as above is



declared, it ought to bee measured (according to the rule of Triangles) in two parts; because there are two Triangles in that land. So by yoose ye shall finde in the upper i. m. l. one Acre, 3. Roddes, and five Dayworks: in the other i. k. l. one Acre. Thus I gather the whole content of that Land, to be two Acres, thre Roddes, and five Dayworks.

More

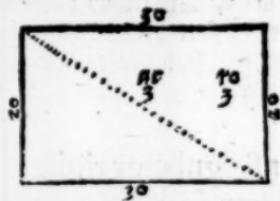
# measuring of Land.

4

None otherwise of the adioynd n. o. p. q. and all other figures following: and other whatsoever they are, that by any means may be brought into Triangles.

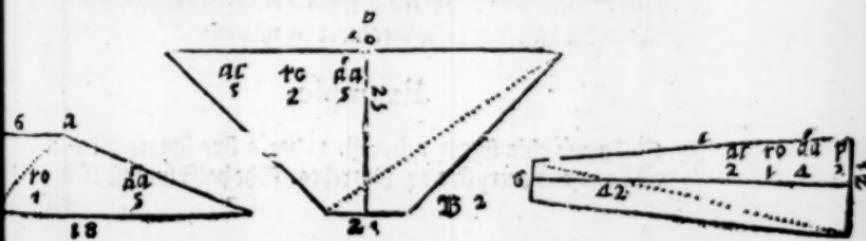
Furthermore know that the figure i. k. l. m. is readily thus measured. Adde the Peaches of both the hanging Lines together: so haue yee 23. With this number, and with halfe the Peaches of the side, i. l. which hee cutteth squirewise, being 10. Peaches, enter your Table. So is found as afors.

These two figures following may also bee thus measured, otherwise then by the rule of Triangles. Enter your Table with their conuenient length and breadth. So shall you finde the contents of all such.



These thre figures following, although they may be measured by the rule of Triangles, yet for quicker spedde, they haue also their proper measuring as ensuet.

Lay together the two sides which are parallels of the first figure a. that is 6. and 18. making 24. the halfe is 12. the breadth 5. Enter with 5. and 12. your table. So haue you one rood, and fife dayworks. For the other two b. c. and such like, ioyn the heads or ends in one:and enter your table with halfe of those Peaches, and with the whole number of the middle line.



# The Art of

## How by supputation to measure all triangled Land.

To measure  
triangled land  
by supputa-  
tion.

Foure rules  
following.

Dyne all the sides together: take halfe out of that halfe, pull  
every side, noting the difference. Then multiply the differen-  
ces, the one in the other, and the third difference augment in the  
product. That which increaseth, multiply in the halfe of all  
the sides loyned. Then the Radix of the surmounting summe  
is the content of that Triangle.

Now rest foure Rules to bee treated of. The first for all  
manner Regular square Superficies. The second for round  
Land, and her parts. The third for Steepleys, Columnnes,  
Globes, and their parts. The last for Mountaines and Val-  
lepes. Here they shall in order follow.

A rule for all manner Regular or right  
squared Land of many sides, as  
5.6.7.8.9.10.20.100,&c.

### *The iiiij. Chapter.*

To measure  
land of many  
sides.

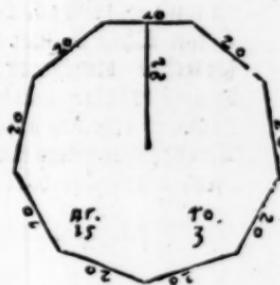
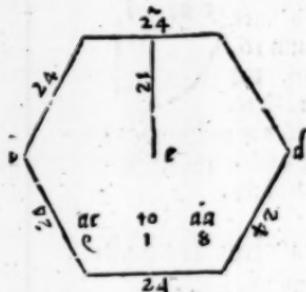
**M**easure and lay all the sides together, taking the  
halfe number of Pearches there contained. Then  
draw a right hanging line from the Center or  
middest of that figure, or the middest of some one  
side: And with that length and the other, enter  
your Table. Note that the Triangle of all sides like, and the  
Quadrat figure are also measured by this rule.

### Example.

**S**uppose this figure a. b. c. d. to bee a sixe square piece of  
Land, and every side 24. Pearches. The halfe summe of all

all sides is 72. Pearches: the right hanging pricked line a. c.  
21. Pearches. With these two numbers ye must enter your  
Table of account following hereafter; and doe as is opened in  
the declaration there adioyned, when Numbers surmount the  
Table as they doe here.

So shall ye finde 9. Acres, 1. Rood, and 8. Daywoikes,  
the content of this figure a. b. c. d. Euen thus is the other  
nine squared figures measured, and such like.



### A Rule for round Land, and the parts thereof.

#### The v. Chapter.

 Also the Diameter multiplied in halfe the Cir. Archimedes in  
cunference, sheweth the content of any Circle. libello circuli  
mensurationis.

Or thus more plainly: Ye shall enter your  
Table with halfe the number of Pearches of the  
whole Circumference or compass, and with the  
number of halfe the Diameter or breadth. So haue yee the  
content.

# The Art of

## Ensample.

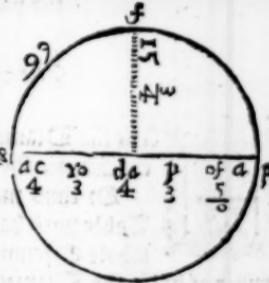
Suppose a piece of land, whereof the compasse is 100. pearches, the breadth 32. Pearches, I would know how much Land is in this figure. Enter your table with halfe the compasse, that is 50. and with halfe the breadth, that is 16. Pearches. Because in the table I cannot finde 50. for the greatest length is 40. (therefore I enter with 40.) and 16. So is found fourre Acres. Then I enter againe with 16. Pearches remayning, and 16. the breadth, as before, that bringeth 1. Acre.  
Now to conclude by addition of one and fourre, I finde fine Acres in that round Land, whose halfe compasse is fifty Pearches, and the breadth sixteene Pearches.



### How parts of Pearches are to be counted in measuring.

For perfect knowledge and use of this table following, when parts of Pearches are adioyned, note well this other example that ensueteth, and also what is said of the declaration annexed unto the table, when parts of Pearches are in the length, breadth, or both.

Imagine f.g. h. to be a round piece of Land: I finde by measure the whole compasse, 99. Pearches. The halfe is  $49\frac{1}{2}$ . The hanging Line or halfe breadth is  $15\frac{3}{4}$ . Enter your table with the whole Pearches, that is 49. and 15. leaving out  $\frac{1}{2}$ . and  $\frac{3}{4}$ . which were but parts of Pearches. So have



# measuring of Land. 6

ye 4. Acres, 2. Roods, 3. Dayworokes, and 3. Pearches. For those parts of Pearches omitted, at your first entering the table, woxke thus: The halfe Pearch, Quarter, or other part of a Pearch in the length, must be reckoned by themselves in the whole breadth, and those of the breadth contrariwise in the length. If there be such odde parts in both, then reckon them of the length in the whole breadth, and them of the breadth in the whole length, ioyning to the other afore-gotten, remembryng the product of the one fraction multiplied in the other, to bee pulled from the encrease. To make this matter plaine, I will take this last example before. The one number wherewith I shoule haue entered my table, was  $49\frac{1}{2}$ , the other  $15\frac{3}{4}$ . I found first by entering with  $49$ , and  $15$ , (omitting the odde parts) 4. Acres, 2. Roodes, 3. Dayworokes, and 3. Pearches. Now for the encrease of the Parts of Pearches left out. I must (as I said) reckon them of the length in the breadth, and contrariwise them of the breadth in the length. Halfe  $15\frac{3}{4}$ , is 7. Pearches, and  $\frac{1}{4}$ . Three quarters of  $49$ , is  $37$ . Pearches,  $\frac{1}{4}$ . Which added, makes 45. Pearches. This adioyned to the number afore-gotten, bringeth the whole content of the round figure, which is 4. Acres, 3. Roods, 4. Dayworokes, 3. Pearches, and  $\frac{1}{4}$  of a Pearch, the product of the one fraction multiplied in the other subducted. What must be done when the numbers wherewith ye shoule enter, exceede your table, counsell the declaration of your table there adioyned.

## Of the halfe Circle.

**F**OR this halfe circle, enter the table with halfe the compasse, & with halfe the Diameter of the circle, or with the length of the pricked hanging line, k. l. So the content of this halfe Circle is 2. Acres, 1. Rood, 7. Dayworokes, 1. Pearch, and  $\frac{1}{3}$  of a Pearch.



To measure  
halfe circled  
Land.

Another

# The Art of

## Another example of Portions and parts of a Circle.

Suppose n. m. o. following, were a part of a circle or piece of Land, whose Content ye desired. The whole Compasse of the Circle which this portion representeth, is (as aforesaid) 99. Peaches: his Diameter or breadth 3 I.  $\frac{1}{2}$ . The pricked Arke or Compasse, n.m.o. is 74. Now with the halfe Breadth or Semidiameter of the Circle, 15.  $\frac{1}{4}$ . and with 37. the halfe of the pricked Compasse, enter your Table. So haue ye 3. Acres, 2. Roodes, 5. Dayworikes, 2. Peaches, and  $\frac{1}{4}$  of a Peach, the Content of the piece of Land full of prickes, to the sides of the Triangle pricked.

If ye desire to know the sum of Peaches in the other portion beneath the Triangle, separated by the Line m. o. ye must adde the Content of the Triangle (which is 3. Roodes and  $\frac{1}{4}$  of a Peach, found by the Rule of Triangles) to the Acres and Peaches before searched. So haue ye 4. Acres, one Roode, 5. Dayworikes, three Peaches, and  $\frac{1}{4}$  of a Peach. This subtracted or pulled from the number contained in the whole Circle, the remaine is the Peaches included in the small piece beneath the Triangle: That is, 1. Roode, 36. Peaches, and  $\frac{1}{4}$  of a Peach.



## How mixed Figures are measured.

Land com-  
pounded of  
circles, or his  
parts.

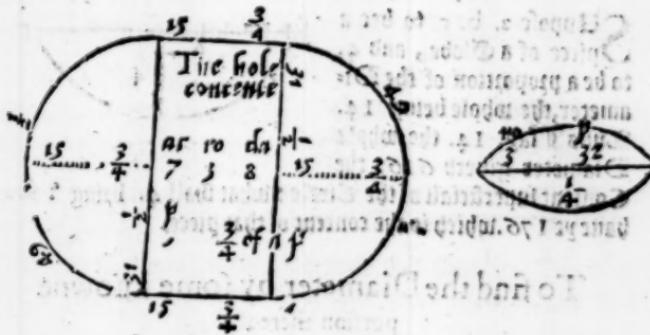
I thinke none now will doubt how these two figures following are measured, because they are made of portions of parts of Circles, whose measure is before sufficienly open-

ned

# measuring of Land.

7

new, the one consisting of two halfe Circles, and a Quadrangle; the other being the portions of the Circle, i.m.d. doubled.



If any euill fashioned Land chance to be measured; which requireth to bee brought into many Triangles, to save labour, yee may adde some portion unto that, and make it square, or otherwise. So let it then bee measured: and after, from the product pull away that yee added: the remaine is the Content.

## To finde the content superficial of Steeple, Columnes, Globes, and their parts.

**T**O the Arithmetician, I say: so picked Steeple, multi-  
plied the whole side in halfe the Circumference of the Base,  
adding the plaine of that Base. For pillars: augment the Cir-  
cumference of the Base in the Heighes, putting to the plaine  
of both bases. For Globes, the diameter in the Circumference  
multiplied. Even so of fragments or parts. Let them that bo  
voide of Arithmetike enter my Table of account following,  
with such numbers as I now willed the Arithmetician to mul-  
tiply, not forgetting what I have before written. So I serue  
their turne.

To measure  
Steeple, Co-  
lumnes,  
Globes, &c.

C

Or

# The Art of measuring

Or thus by the rule of proportion, the  
parts of a Globe are found.

To measure  
parts of  
Globes.

Suppose a. b. c. to bee a  
piece of a Globe, and 4.  
to be a proportion of the Di-  
ameter, the whole being 14.  
Thus I say, 14. the whole  
Diameter giueth 616. the  
Content superficiale of the Circle : what shall 4. bring ? So  
haue ye 176. which is the content of that piece.



To find the Diameter by some knowne  
portion thereof.

To finde the  
vnknowne Di-  
ameter of a  
Globe.

If ye be ignorant what length the Diameter of the Globe  
is, whose proportion ye haue, the height or part of the De-  
mierc being 4. foote, augment halfe the line a.b. which is 6.  
3. in hinselle, and the product diuide by 4. So haue ye 10. to be  
added to 4. which maketh 14. the whole Diameter.

The true measuring of Moun-  
taines and Valleys.

*The vi. Chapter.*

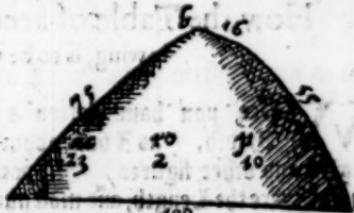
To measure  
Mountaines.



First ye shall measure the circuit of the Foot, or Vale of the Mountaine : then the compasse of the Summite or top, adding them together. So shall ye do of the Acrenes, that is, the going by from the base to the top, ioyning the measure of the longer & short in one. Now take the halfe of the circuit added, & the halfe part of the Acrenes ioyned, and enter your Table: there shall ye see the Content, Example

## Ensample.

A.b.c. is the mountaine : a.c. the circuit or the Hill, being Figure of a  
100. Peaches, b. the top 16. Peaches. Which ioynt together, make 116. b. c.  
ther, make 116. b. c.  
the one Acreuse is 55.  
Peaches : the other  
75. These added  
make 130. The halfe  
of the circuitis is 58.  
the halfe of the Acre-  
ses 65. with these two  
summes yee shall en-  
ter your Table of account, where ye shall finde 23. Acres, 2.  
Roddes, and 10. Peaches, the true content of this figured hill.



## Of the Valley.

**A**s in the Mountaine yee measured the circuit or compass  
of the Vale or Foute : so here contrary yee shall meare  
round about the circuit or compass of the height of the Val-  
ley. And as yee got the measure or compass of the top of the  
Mountaine, so meare the circuit of the depth of the Val-  
ley. In like manner as yee measured the Acreuse, that is, the  
going vp from the foote to the top: so meare the Discente or  
going downe of the Hill, to the depth of the Valley. The rest all  
woake, as I haue shewed you in measuring the Mountaine.  
For more plain-  
nesse, behold this  
ensample of li-  
gure. If ye lay  
together the cir-  
cuites of the  
height & depth,  
which is 210.

To measure  
Valleyes.

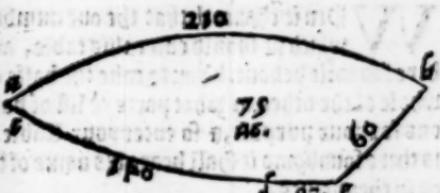


Figure of a  
Valley.

and 30. taking the halfe part of those two Circuites, making

## The Art of measuring

an 120: then the two Assenses 140. and 60. added in one product 200. the halfe thereof being 100: with this and 120. the other halfe of the Circuitte, ye may enter your Table. That doing, loe 75. Acres.

### How the Table of account now following, is to be vsed.

What is to bee done when numbers, with which you shoulde enter, exceede your Table.

**V**hen you haue gotten a convenient Length and Breede, (as I haue aboue declared by divers Triangles and other figures) then you shall enter this Table. Take there the Length, and most number of Pearches in the higher margine, which beginneth at 1. and endeth righward at 40. Looke the other latime of Pearches (I meane the breede) in the right side and hanging margine, from 1. descending to 30. Now at the meeting of the lines, where the one answereth the other nicely in a square, you shall finde the Acres, Roodes, Day workes, and Pearches. Note that the first numbers set on the left side, and upper part in any square, signifieth the number of Acres. The figure 1. set in the upper part, and right side, doth betoken a Rodde: the figure 2. there two Rodds. 3. three Roddes. And the figure in the left side beneath, signifieth a Day worke; or Day workes. A figure in the lower part righward declareth Pearches.

### A Declaration adioyned.

**V**hen it chanceth that the one number or both with the which ye shoulde enter this table, are greater then any here found: it behoueth you to take the halfe of the one, and the whole of the other, or what parts ye list of both, most commodious for your purpose, & so enter your Table. Looke then what is there found, and it shall beare his name of the parts multipled in themselves.

Ensample

## Ensample.

Suppose the number with the which ye shoulde enter your Table to bee 130. Pearches in length, and the breadth 60, neither of these may be found in the margins: wherefore I take the third part of an 130. which is 34. Pearches, and one remaneth.

The halfe 60 that is 30. I finde with entring them at the common meeting, & Acres, 1. Roode, and 5. Day workes. This summe must haue his name of the parts augmented in themselues. I tooke the third part of the one, and halfe the other number, therefore 2. must bee multiplied in 3. or contrarie: so haue ye sixe, which signifieth that ye haue found by entring, but the sixth part of the number ye shoulde finde. Wherefore I must take this summe tofore found (besyng Acres, 1. Roode, and 5. Dayworkes) sixe times as much. So haue ye 33. Acres, & one Roode. For the Pearch remaining in length, reckon him in the bredth (as is afore declared) in the fifth Chapter of the Remainders: so haue ye 60. Pearches more to be added. So the encrease of these two numbers, 103. and 60. amount to 38 Acres, two Roodes and 5. Day workes. Thus any manner length and bredth is reduced to this Table following, which sufficeth.

Thus with few words is ended the certaine measuring of all manner Land, touching the Superficiall Contents. Wherefore now shall follow the true measuring of Timber, Stone, Steeples, Pillers, Globes, according to their Crassitude.

Such as are altogether ignorant of Arithmetike, may rec-  
ken by our English coyne, allowing for every Pearch in length  
or bredth a penny, and so every Parke makes an Acre, every  
Noble halfe an Acre, euery forty pence or halfe Noble, a roode,  
and every penny a square Pearch. And so by memorie without  
Tables, may in some rude and grosse manner, cast vp reasonable  
lye iust the true contents of all Closes, Meadowes, Parches,  
Hils or Valleys.

Looke what I  
have shewed  
in the Chapter  
of parts, that  
understand  
here of whole  
Peaches,  
left substra-  
ting, &c.

Q. **May** bisonicione

1. **May** bisonicione  
2. **May** bisonicione  
3. **May** bisonicione  
4. **May** bisonicione  
5. **May** bisonicione  
6. **May** bisonicione  
7. **May** bisonicione  
8. **May** bisonicione  
9. **May** bisonicione  
10. **May** bisonicione  
11. **May** bisonicione  
12. **May** bisonicione  
13. **May** bisonicione  
14. **May** bisonicione  
15. **May** bisonicione  
16. **May** bisonicione  
17. **May** bisonicione  
18. **May** bisonicione  
19. **May** bisonicione  
20. **May** bisonicione  
21. **May** bisonicione  
22. **May** bisonicione  
23. **May** bisonicione  
24. **May** bisonicione  
25. **May** bisonicione  
26. **May** bisonicione  
27. **May** bisonicione  
28. **May** bisonicione  
29. **May** bisonicione  
30. **May** bisonicione  
31. **May** bisonicione



## TO THE READER.

**T**commeth commonly to passe, that Carpenters, Masons, and such like Artificers, are put either to measure timber every way square, or squared logs, broader on the one side then on the other: yea many times mutilate or vnpesfect stufte. Sometimes three, fife, tenne, or twenty, square in the head, and so through: oftentimes round Stone or timber with hollowed, &c. Afore I shew vnto them what must be done with such pieces of timber or Stone, to get their true measure, my desire shalbe that such Craftsmen will leaue to be heady or selfe willed: yea so greedily to sticke to their corrupted rules, that vitterly they refuse to be taught.

Both learning and experience declareth vnto me, that the grounds which the best of them haue, are false. To open how and where, it needeth not: neither doth it appertaine to instruction, onely it may suffice him that liketh the true way, here to receiue it appointed to him. Yet to satisfie and content him which will not beleue any such errors or false grounds to bee, I say (and truly) that the Ruler of Timber measure, which the most part of them hath, is not made by right Art: Besides that, their craft in seeking the Square of some Timber is very false. They vse in measuring, to lay the broader and narrower sides together in a summe, and to take the halfe of that number for the Square. Then they seeke this vntrue Square vpon the false Ruler, and so measuring the Timber, they conclude of it vntruly.

As

## To the Reader.

In a Foote  
square is con-  
tained 172.  
Inches.

As this is corrupted, so are other Grounds which they take to be infallible. Now to the purpose : touching the correction of those Errors, with other not mentioned, whereby true measuring may ensue, this way shall be taken. After I haue opened how you must handle all such fashioned Timber (as afore is spoken of) there shall follow a Table in which ye may finde (as I will declare) the Square of any Stone or Timber. That knowne, it is requisite to haue another Table immediately following, which may appoint to all true Squares from 1. to 6. inches, the iust length to make a foote every way square. With the length agreeable to your Square, your Logge must be measured. And as oft as ye finde it from the one end to the other of your Timber, so oft ye may conclude the foote Square to be contained in that timber Logge, or Stone : that is, so many Square Feete there to be included. This Table of Timber measure standeth in the place of a good Ruler, well decked with true measures. By this ye may make or correct Rulers at pleasure, as after appeareth.

*Now orderly followeth the true measuring of all fashioned Timber or stone aforesaid.*

G	42	43	44	45	46	47
	Partes	Partes	Partes	Partes	Partes	Partes
31	67580	68856	70111	71345	72557	73747
32	67601	77	32	65	77	67
33	23	98	53	86	97	86
34	44	68919	73	71406	72617	73806
35	66	40	94	26	37	25
36	87	61	70215	47	57	45
37	67709	83	36	67	77	65
38	30	69004	56	87	97	84
39	51	25	77	71508	72717	73904
40	73	46	98	28	37	23
41	94	67	70318	48	57	43
42	67815	88	39	69	77	63
43	37	69109	60	89	97	82
44	58	30	80	71609	72817	74002
45	80	51	70401	30	37	21
46	67901	72	22	50	57	41
47	22	93	42	70	76	60
48	44	69214	63	91	96	80
49	65	35	84	71711	72916	74100
50	86	56	70504	31	36	19
51	68008	77	25	51	56	39
52	29	98	45	72	76	58
53	50	69319	66	92	96	78
54	73	40	87	71812	73016	97
55	94	61	70607	32	36	74217
56	68114	82	28	53	55	36
57	35	69403	48	73	75	56
58	56	23	69	93	95	75
59	78	44	90	71913	73115	95
60	99	65	70710	33	35	74314

G	48	49	50	51	52	53
m	Partes	Partes	Partes	Partes	Partes	Partes
1	74333	75490	76623	77732	78818	79881
2	53	75509	41	51	36	98
3	72	28	60	69	54	79916
4	92	47	79	87	72	33
5	74411	66	97	77806	90	51
6	31	85	76716	24	78908	68
7	50	75604	35	42	26	85
8	70	23	53	60	44	80003
9	89	42	72	79	61	20
10	74508	61	91	97	79	38
11	28	80	76809	77915	97	55
12	47	99	28	33	79015	73
13	66	75718	46	52	33	90
14	86	37	65	70	51	80107
15	74605	56	84	88	68	25
16	25	75	76902	78006	86	41
17	44	94	21	24	79104	60
18	63	75813	39	43	22	77
19	83	32	58	61	40	94
20	74702	51	77	79	57	80212
21	21	70	95	97	75	29
22	41	89	77014	78115	93	47
23	60	75908	32	33	79211	64
24	79	27	51	52	28	81
25	99	46	69	70	46	99
26	74818	64	88	88	64	80316
27	37	83	77106	78206	82	31
28	57	76002	25	24	99	51
29	76	21	43	42	79317	68
30	95	40	62	60	35	85

G	48	49	50	51	52	53
m	Partes	Partes	Partes	Partes	Partes	Partes
31	74914	76059	77180	78278	79353	80402
32	34	78	99	97	70	20
33	53	97	77217	78315	88	37
34	72	76116	36	33	79406	54
35	91	34	54	51	23	72
36	75011	53	73	69	41	89
37	30	72	91	87	59	80506
38	49	91	77310	78405	76	23
39	68	76210	28	23	94	41
40	88	29	47	41	79512	58
41	75107	48	65	59	29	75
42	26	66	84	77	47	92
43	45	85	77402	95	64	80610
44	64	76304	20	78513	82	27
45	83	23	39	31	79600	44
46	75203	42	57	49	17	61
47	22	60	76	67	35	78
48	41	79	94	85	52	96
49	60	98	77512	78603	70	80713
50	79	76417	31	21	88	30
51	99	35	49	39	79705	47
52	75318	54	67	57	23	64
53	37	73	86	75	40	81
54	56	92	77604	93	58	98
55	75	76510	22	78711	75	80816
56	94	29	41	29	93	33
57	75413	48	59	47	79811	50
58	32	67	77	65	28	67
59	51	85	96	83	46	84
60	70	76604	77714	78801	63	80901

G	54	55	56	57	58	59
III	Partes	Partes	Partes	Partes	Partes	Partes
1	80918	81931	82920	83882	84820	85731
2	35	48	36	98	35	46
3	52	65	52	83914	51	61
4	70	81	68	30	66	76
5	87	98	85	46	81	91
6	81004	82015	83001	61	97	85806
7	21	31	17	77	84912	21
8	38	48	33	93	27	36
9	55	65	49	84009	43	51
10	72	81	66	25	58	66
11	89	98	82	40	73	81
12	81106	82114	98	56	89	96
13	23	31	83115	72	85004	85910
14	40	48	30	88	19	25
15	57	64	46	84103	35	40
16	74	81	63	19	50	55
17	91	97	79	35	65	70
18	81208	82214	95	51	81	85
19	25	30	83211	66	96	86000
20	42	47	27	82	85111	14
21	59	64	43	98	26	29
22	76	80	59	84213	42	44
23	93	97	76	29	57	59
24	81310	82313	92	45	72	74
25	27	30	83308	60	87	89
26	43	46	24	76	85203	86103
27	60	63	40	92	18	18
28	77	79	56	84370	33	33
29	94	96	72	23	48	48
30	81411	82412	88	39	64	62

G	54	55	56	57	58	59
m	Partes	Partes	Partes	Partes	Partes	Partes
31	81428	82429	83404	84354	85279	86177
32	45	45	20	70	94	92
33	62	62	36	86	85309	86207
34	79	78	52	84401	24	21
35	95	94	68	17	39	36
36	81512	82511	84	32	55	51
37	29	27	83500	48	70	66
38	46	44	16	63	85	80
39	63	60	32	79	85400	95
40	80	77	48	95	15	86310
41	96	93	64	84510	30	24
42	81613	82609	80	26	45	39
43	30	26	96	41	60	54
44	47	42	83612	57	76	68
45	64	58	28	72	91	83
46	80	75	44	88	85506	98
47	97	91	60	84603	21	86412
48	81714	82708	76	19	36	27
49	31	24	92	34	51	42
50	48	40	83708	50	66	56
51	64	57	24	65	81	71
52	81	73	40	81	96	85
53	98	89	55	96	85611	86500
54	81814	82806	7	84712	26	15
55	31	22	87	27	41	29
56	48	38	83803	43	56	44
57	65	54	19	58	71	58
58	81	71	35	73	86	73
59	98	87	51	89	85701	87
60	81915	82903	67	84804	16	86602

G	60	61	62	63	64	65
M	Partes	Partes	Partes	Partes	Partes	Partes
1	86617	87476	88308	89113	89892	90643
2	31	90	22	27	89904	55
3	46	87504	35	40	17	67
4	60	18	88349	53	30	79
5	75	~ 32	62	89166	43	92
6	89	87546	76	79	89955	90704
7	86704	60	90	92	68	16
8	18	74	88403	89206	81	28
9	33	88	17	19	93	41
10	47	87602	30	32	90006	90753
11	62	16	44	45	19	65
12	76	30	88458	89258	31	77
13	91	44	71	71	44	89
14	86805	87658	85	84	90057	90802
15	19	72	98	97	69	14
16	34	86	88512	89310	82	26
17	48	87700	25	24	95	38
18	63	14	39	37	90107	90850
19	77	28	52	50	20	62
20	91	42	88566	89363	32	75
21	86906	87756	79	76	45	87
22	20	70	93	89	90158	99
23	35	84	88606	89402	70	90911
24	49	98	20	15	83	23
25	63	87812	33	28	95	35
26	78	26	47	41	90208	47
27	92	40	88660	89454	20	90959
28	87006	53	74	67	33	71
29	21	67	87	80	46	84
30	35	87881	88701	89493	90258	96

G	60	61	62	63	64	65
	Partes	Partes	Partes	Partes	Partes	Partes
643	31	87049	87895	88714	89506	90271
55	32	64	87909	27	19	83
67	33	78	23	41	32	96
79	34	92	37	54	45	90308
92	35	87107	51	88768	89558	21
704	36	21	87964	81	71	33
16	37	35	78	94	84	46
28	38	49	92	88808	97	90358
41	39	64	88006	21	89609	70
753	40	78	20	35	22	83
65	41	92	33	48	35	95
77	42	87206	47	88861	48	90408
89	43	21	88061	75	89661	20
802	44	35	75	88	74	33
14	45	49	89	88901	87	45
26	46	63	88102	15	89700	90457
38	47	78	16	28	12	70
350	48	92	30	41	25	82
62	49	87306	44	88954	38	95
75	50	20	88157	68	89751	90507
87	51	34	71	81	64	19
99	52	48	85	94	77	32
911	53	63	98	89008	89	44
23	54	77	88212	29	89802	90556
35	55	91	26	34	35	69
47	56	87405	40	47	28	81
959	57	19	53	89060	41	93
71	58	33	88267	74	89853	90606
84	59	47	81	87	66	18
96	60	61	94	89100	79	30
						91354

G	66	67	68	69	70	71
	Partes	Partes	Partes	Partes	Partes	Partes
1	91366	92061	92729	93368	93979	94561
2	78	73	40	78	89	70
3	90	84	51	89	99	80
4	91401	95	61	99	94009	89
5	13	92107	92772	93410	18	99
6	25	18	83	20	28	94608
7	37	29	94	30	38	17
8	91448	41	92805	41	48	27
9	60	92152	16	93451	94058	36
10	72	63	26	61	63	46
11	84	75	37	72	78	94655
12	95	86	92848	82	88	64
13	91507	97	59	92	97	74
14	19	92208	70	93503	94107	83
15	31	20	80	13	17	93
16	42	31	91	23	27	94703
17	91554	42	92902	34	37	11
18	66	92253	13	93544	47	21
19	77	65	24	54	94156	30
20	89	76	34	64	66	39
21	91601	87	92945	75	76	94748
22	12	98	56	85	86	58
23	24	92309	66	95	95	67
24	36	21	77	93605	94205	76
25	91647	32	88	16	15	86
26	59	43	99	26	25	95
27	71	92354	93009	36	34	94804
28	82	65	20	46	44	13
29	94	76	31	57	94254	23
30	91706	92387	93041	67	64	33

G	66	67	68	69	70	71
M	Partes	Partes	Partes	Partes	Partes	Partes
31	91717	92399	93052	93677	94273	94841
32	29	92410	62	87	83	50
33	40	21	73	97	93	60
34	52	32	84	93707	94302	69
35	91763	43	94	18	32	94878
36	75	92454	93105	28	22	87
37	87	65	16	38	31	96
38	98	76	26	93748	41	94905
39	91810	87	37	58	94351	15
40	21	98	93147	68	60	24
41	33	92509	58	78	70	33
42	44	20	69	88	80	42
43	91856	32	79	98	89	51
44	67	43	90	93809	99	94960
45	79	92554	93200	19	94408	69
46	90	65	11	29	18	79
47	91902	76	21	39	28	88
48	13	87	32	93849	37	97
49	24	98	93242	59	47	95006
50	36	92609	53	69	94456	15
51	91947	20	63	79	66	24
52	59	30	74	89	75	33
53	70	41	84	99	85	42
54	82	92652	95	93909	94	51
55	93	63	93305	19	94504	95060
56	92004	74	16	29	13	69
57	16	85	26	39	23	78
58	27	96	37	93949	32	87
59	39	92707	47	59	42	96
60	92050	18	93358	69	94551	95105

G	72	73	74	75	76	77
fit	Partes	Partes	Partes	Partes	Partes	Partes
1	95114	95638	96134	96600	97036	97443
2	23	47	42	07	43	50
3	32	55	50	15	50	96
4	41	64	58	22	75	63
5	50	95672	66	30	64	69
6	95159	81	74	37	97071	76
7	68	89	82	45	78	82
8	77	98	90	52	85	89
9	86	95706	98	60	92	95
10	95	15	96205	67	99	97502
11	95204	23	13	74	97106	08
12	12	31	21	82	13	14
13	21	40	29	89	20	21
14	30	95748	37	97	27	27
15	39	57	96245	96704	34	97514
16	95248	65	53	11	97141	40
17	57	73	61	19	48	47
18	66	95782	69	26	54	53
19	74	90	96277	34	61	59
20	83	98	84	96741	97168	97566
21	92	95807	92	48	75	71
22	95301	15	96300	56	82	78
23	10	23	08	63	89	85
24	19	32	16	70	96	91
25	27	40	24	96778	97202	98
26	36	95848	96331	85	09	97604
27	45	57	39	92	16	10
28	54	65	47	96800	23	16
29	62	73	55	07	30	23
30	95371	95881	96363	14	97236	97629

G	72 Partes	73 Partes	74 Partes	75 Partes	76 Partes	77 Partes
31	95380	95890	96370	96822	97243	97635
32	89	98	78	29	50	42
33	97	95906	86	36	57	48
34	06	14	94	43	64	54
35	15	23	96401	51	70	60
36	95424	31	09	96858	97277	67
37	32	39	17	65	84	97673
38	41	95947	24	72	91	79
39	50	56	32	79	97	85
40	95458	64	96440	87	97304	92
41	67	72	48	94	11	98
42	76	95980	55	96901	17	97704
43	84	88	63	08	24	10
44	93	96	96471	15	31	16
45	95501	96004	78	23	97337	23
46	10	13	86	30	44	29
47	19	21	94	96937	51	97735
48	27	29	96501	44	57	41
49	36	37	09	51	64	47
50	95545	96045	16	58	97371	53
51	53	53	24	65	77	60
52	62	61	96532	96973	84	97766
53	70	69	39	80	90	72
54	79	96077	47	87	97	78
55	95587	85	54	94	97404	84
56	96	94	62	97001	10	90
57	95604	96102	96569	08	17	96
58	13	10	77	15	23	97802
59	21	18	85	22	30	08
60	30	26	96592	97029	97437	14

G	78	79	80	81	82	83
III	Partes	Partes	Partes	Partes	Partes	Partes
1	97820	98168	98485	98773	99030	99258
2	26	73	90	77	34	61
3	32	79	95	82	38	65
4	38	84	98500	86	42	68
5	44	90	05	91	46	72
6	97850	95	10	98795	99050	99275
7	56	98201	15	98800	54	79
8	62	06	20	04	58	82
9	68	12	98525	09	62	85
10	74	17	30	13	66	89
11	97880	22	35	18	99070	99293
12	86	98228	40	98822	74	96
13	92	34	45	27	78	99300
14	98	39	98550	31	82	02
15	97904	45	55	36	86	06
16	10	50	60	40	99090	10
17	16	98255	65	98844	94	13
18	22	61	70	49	98	99317
19	28	66	98575	53	99102	20
20	97934	72	80	58	06	23
21	39	77	85	62	09	27
22	45	98282	89	98866	13	30
23	51	88	94	71	17	99333
24	57	93	99	75	99121	37
25	97963	98	98604	79	25	40
26	69	98304	09	84	29	43
27	75	09	14	98888	33	47
28	80	14	18	92	36	99350
29	86	20	23	97	40	53
30	97992	98325	98628	98901	99144	57

G	78	79	80	81	82	83
m	Partes	Partes	Partes	Partes	Partes	Partes
31	97998	98330	98633	98905	99148	99360
32	98004	36	38	10	52	63
33	09	41	42	14	55	67
34	15	46	47	18	59	70
35	21	51	52	22	63	73
36	27	98357	98657	98927	99167	99376
37	98032	62	61	31	70	80
38	38	67	66	35	74	83
39	44	72	71	39	78	86
40	50	78	76	44	82	89
41	55	98383	98680	98948	99185	99392
42	98061	88	85	52	89	96
43	67	93	90	56	93	99
44	72	98	94	60	96	99402
45	78	98404	99	65	99200	05
46	84	09	98704	98969	04	08
47	89	14	08	73	07	11
48	95	19	13	77	11	15
49	98101	24	18	81	15	99418
50	06	98429	22	85	99218	21
51	12	34	98727	98990	22	24
52	18	40	32	94	25	27
53	23	45	36	98	29	30
54	98129	50	41	99002	33	99413
55	34	98455	45	06	99236	36
56	40	60	98750	10	40	39
57	46	65	55	14	44	43
58	51	70	59	18	47	46
59	57	75	64	22	51	99449
60	98162	98480	98761	99025	99256	52

G	84	85	86	87	88	89
m	Partes	Partes	Partes	Partes	Partes	Partes
1	99455	99622	99758	99864	99939	99985
2	58	24	60	65	40	85
3	61	27	62	67	41	86
4	64	29	64	68	42	86
5	67	32	66	70	43	87
6	99470	99624	99768	99871	99944	99987
7	73	37	70	73	45	88
8	76	39	72	74	45	99988
9	79	41	74	76	46	88
10	82	44	76	77	47	89
11	99485	99646	99778	99878	99948	99989
12	88	49	80	79	49	90
13	91	51	82	80	50	90
14	93	54	83	82	51	99991
15	96	56	85	83	52	91
16	99	99658	99787	99884	99953	91
17	99502	61	89	86	54	92
18	05	63	91	88	55	92
19	08	66	93	90	55	92
20	11	68	95	91	56	99993
21	14	99670	99797	99893	99957	93
22	99517	73	99	94	58	93
23	19	75	99800	95	59	94
24	22	77	02	97	60	94
25	25	80	94	98	61	94
26	28	99682	06	99	99961	99995
27	99521	84	08	99900	62	95
28	34	87	99809	02	63	95
29	36	89	11	03	64	95
30	39	91	13	99904	99964	96

89	G	84	85	86	87	88	89
	Partes						
9985	31	99542	99694	99815	99906	99965	99996
85	32	45	96	17	07	66	96
86	33	47	98	18	08	67	96
86	34	50	99700	20	09	67	97
87	35	53	03	22	11	68	97
87	36	99556	05	99823	99912	99969	97
88	37	58	07	25	13	70	99997
988	38	61	09	27	14	70	97
88	39	64	99711	29	15	71	98
89	40	67	14	30	17	72	98
89	41	99569	16	99832	99918	99972	98
90	42	72	18	34	19	73	98
90	43	75	20	35	20	74	99998
991	44	77	99722	37	21	74	98
91	45	80	25	39	22	75	99
91	46	99583	27	99840	99924	99976	99
92	47	85	29	42	25	76	99
92	48	88	31	44	26	77	99
92	49	91	99733	45	27	78	99999
993	50	93	35	47	28	78	99
93	51	99596	37	99848	99929	79	99
93	52	98	39	50	30	80	99
94	53	99601	42	52	31	81	99
94	54	04	99744	53	32	81	99
94	55	06	46	55	33	82	99999
995	56	09	48	99856	99934	99982	99
95	57	11	50	58	35	83	99
95	58	99614	52	59	37	83	99
95	59	16	54	61	38	84	100000
96	60	19	56	62	99939	99984	100000





## L.D. To the Reader.



Though (gentle Reader) many excellents in Geometry,  
upon infallible groundes, haue put forth divers most  
certaine and sufficient Rules, touching the measuring  
of all manner Superficies: yet in that the Art of num-  
bring hath been required, yea, chiefly those Rules hid,  
and as it were locked vp in strange Tongues, they doe profit (or haue  
furthered) very little the most part: Certes nothing at all, the Land-  
meeter, Carpenter, Mason, wanting the aforesaid. For their sakes  
I am here pronoked not to hide, but to open, and so encrease the Ta-  
lent which I haue received: yea, to publish in this our Tongue very  
shortly (if God giue life) a volume containing the flowers of the Sci-  
ences Mathematicall, largly applied to our outward practice, pro-  
fitably pleasant to all manner men in this Realme. In the meane time  
I shall desire the Artificers aboue named, to bee contented with this  
little Booke (a taste of my good will towards them) which I wish even  
so to further the Readers, as I know it sufficient for the true measu-  
ring and ready account of all manner Land, Timber, Stone, Boord,  
Glasse, Panement, &c.

Here mine advice shall bee to these Artificers that will profit in  
this, or any of my bookes, now published, or that hereafter shall bee,  
first confusely to reade them thorow, then with more judgement.  
Reade at the third reading, wittily to practise: So few things shalbe  
unknowne. Note, oft diligent reading, ioyned with ingenuus pra-  
ctice, can shew profitable labour.

Thus most heartily farewell, (loving Reader) to whom I wish  
my selfe present, to further thy desire and  
practice in these.

# THE PLEASANT PROFIT OR content of this little Booke, and in what it exceedeth all other published.



Ther bookes tofore put forth in our English tonge, contained only the bare measuring of Land, Timber, and Boord: how agreeable in all places to the rules of Geometrie, let the learned iudge. Here (gentle Reader) thou shalt plainly perceiue through diligent reading, how to measure truly, and very speedily all manner Land, Timber, Stone, Steeples, Pillers, Globes, Boord, Glasse, Pauement, &c. without any trouble: nor painted with many rules, or obscure termes, nor yet with the multitude of tables, as heretofore hath bin: in which not a few errors were committed: for that cause no iust account might any way be had. Further, ye shall by this booke vnderstand the whole making and comely handling of the Carpenters Ruler, wirth the true measure, &c. And his vse appointed to the ready measuring of all kind of Timber, Stone, Boord, &c. Also the leuellung of grounds, and taking of heights, is pleasantly and diuersly practised by the Ruler. Ye haue here not the common, but the rare vse of the Squire, applied to heights, lengths, &c. And to the finding of the iust houre of the day diuers waies, through the aide of pleasant Tables newly adioyned to my generall Prognostication: by the which the proportion of things, direct or squirewise standing, are by their shadowes knowne.

To conclude, in the end of this Booke is added a Treatise, shewing the making, and vse of an Instrument, by which yee shall get lengths, heights, breadths, widenesse, where or howsoeuer they stand. Other necessarie things are contained in this little volume, which I commit to the diligent Reader.





# DIVERS THINGS CONDVCIBLE TO THE ARTE OF MEASVRING.

---

## *The first Chapter.*



So there are few craftsmen which Character  
haue all the kinds of Arithmetike numerall.  
readily: so I doe suppose none so ignorant, but that they doe, or may  
easily perceiue the simple significations of these characters or figures,  
1. 2. 3. 4. 5. 6. 7. 8. 9. 10. And also their  
strength in the first, second, and third  
roomes placed.

Besides that, they must be familiar with these and such like fractions.

$\frac{1}{2}$ .  $\frac{1}{3}$ .  $\frac{1}{4}$ .  $\frac{1}{5}$ .  $\frac{1}{6}$ .  $\frac{1}{7}$ .  $\frac{1}{8}$ .  $\frac{1}{9}$ .  $\frac{1}{10}$ . The first lefward betokeneth one se-  
cond part of an whole, bee it Pearch, Inch, or any other mea-  
sure: the next, one third, then one senench part: the other en-  
fuing, one sixteenth. So one thirtie and two parts of an Inch.  
Then follow thzee fourths: foure fifths. The last is nine tenths  
of an Inch: that is, nine parts of an Inch, diuided into ten po-  
tions.

These I doe intend to put in my Examples, and in my  
tables and margunes following, to represent parts of Pear-  
ches or Inches. As it I would write halfe an Inch, after  
this

# The Art of

this manner  $\frac{1}{3}$ . Three quarters of an inch thus  $\frac{1}{3}$ . One eight of a Pearch, on this wise  $\frac{1}{8}$ . So of the rest.

It is requisite also here to open what a Pearch, a Day worke, a Roode, and an Acre is.

Although there are diuers opinions engendred through long custome in many places, of the length of a Pearch, (upon which our chiefe matter dependeth) yet there is but one true Pearch by Statute appointed to measure by. Wherein is ordained three Barly cornes dyne and round, to make an inch: twelue Inches, a Foote; three Foote, a Yard: five Yards, Acre.

|                                                                                                                                                      |         |         |
|------------------------------------------------------------------------------------------------------------------------------------------------------|---------|---------|
| $\frac{1}{2}$ . a Pearch : for syze Pearches in length,<br>and fourte in breadth, an Acre. So an Acre<br>by Statute ought to containe 160. Pearches; | 1 — 160 | Length. |
| the halfe Acre 80. Pearches; a Roode,                                                                                                                | 2 — 80  |         |
| commonly called a quarter, 40. Pearches,                                                                                                             | 4 — 40  |         |
| a day worke 4. Pearches. Loe heere<br>the Acre expressed with his length and<br>breedth.                                                             | 5 — 52  |         |
|                                                                                                                                                      | 8 — 20  |         |
|                                                                                                                                                      | 10 — 16 |         |

Instruments  
to measure  
with Poales,  
Cord knotted.  
Profitable  
stafce.

Triangle.

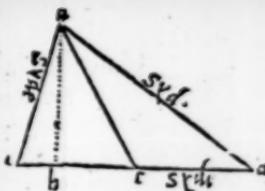
Line falling  
squirewise.

I must not omit here to tell you what thing is meetest to measure Land with. They vse commonly in the countrey two Poales, either of them the length of a Pearch. They are very good: yet for all kinde of Land, a Cord syze Pearches in length, well seared with waxe and rosen, knotted or marked at the end of every Pearch, is more meete and readier. But in my fantasie, the instrument Geometricall, which is put forth in the end of this booke, passeth them all and other, for the exact truth and quickest speed. This Instrument is so generall and auailable to so sundry things, that it alone requireth a large booke, if it shold be sufficiently set forth.

Also I would not haue you ignorant what piece of Land is called a Triangle, which often shall hereafter be named. It is such a fashioned piece as hath (or is imagined to haue) thre sides, and thre Angles onely: whether the sides be equall or otherwise, as this figure sheweth. Againe, note that a line is said to fall Squirewise, when it cutteth any thing, or any of a Triangle full crosse, like unto a Squire: As the hanging  
pricked

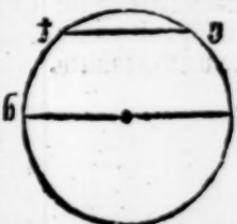
Measuring

yscked line. a. b. in c. d. the base line of the Triangle. Lo, it cut-  
ter the side squirewise, or full  
crosse in the point b. and not as  
the other line a. c. doth. The  
base of any Triangle is here cal-  
led that side, which is cut squire-  
wise of the hanging line.



Base line.

Concerning a Circle, know, that the compass of any Circle. Circle is named a Circumference: the middle point in him, is Center: the right line h.i. that goeth ouerthwart that Center touching the Circumference on both sides is his Diameter: the halfe of that line, the Semidiameter. Also an Arch is a piece of the Circumference cut away: as ye see the Arch above the line f. g. Also f.g.h.i. in this Circle are named parallels: for that they differ equally in al places, the one from the other.



Circumfe-  
rence.  
Center.  
Diameter.  
Semidiameter.  
Arch.  
Parallels.

Note, because practice and experience sheweth me, that there is almost no Land, but it may easily be brought by imagination to a Triangle or Triangles, and so most truly measured: there-  
fore, to be short, this order shall be taken: I will first figure and set afore your eyes Triangled Land, and other which by imagi-  
nation shall bee brought into Triangles. Then I shall teach the true measuring of them: I meane, how to finde a length and breadth, with which ye shall enter the table of account following, where the Acres and oþre Pearches (if there be any) shall ap-  
pear. As these figures are measured, so all Triangled Land, and other brought into Triangles, of what fashion so ever they bee, shall be measured. And because it is requisite for true measuring of all Triangles, to finde a straight hanging line, I shall shew first how that line is to bee found, imagined, or drawne.

How

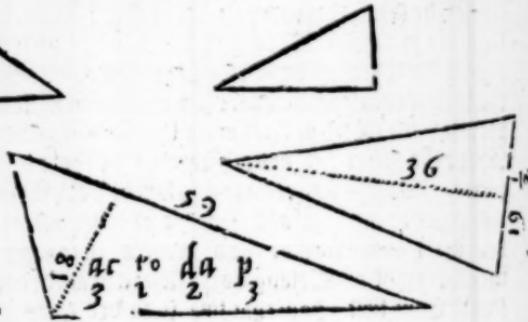
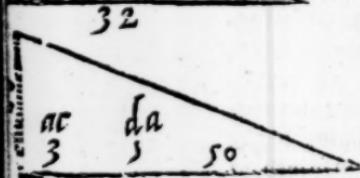
THE 7<sup>TH</sup> CHAP.

## How the right hanging line in Triangles is drawn.

*The 7<sup>th</sup>. Chapter.*

To draw a  
hanging or  
plumbe line.

This straight hanging line in all Triangles is ever  
drawne or imagined from any Angle, cutting some one  
side of that Triangle squarewise : as ye may perceiue the  
picked lines in the Triangles following. By the helpe of  
this line, all Landes of Triangle fashion, are brought to bee  
measured as ensueth.





How Timber or Stone fouresquare  
every way, or broader on the one side  
then on the other, is measured.

*The viij. Chapter.*

**H**o a piece of Timber or Stone, bee either equally square, broader on the one side, then on the other, yee shall take the full measure, I meane, how many Inches the broader side containeth : euen so of the narrower. This done, yee must seeke in the Table of squares following, the measure of the broader side of the Timber or Stone, in the vpper margine of that Table. Then looke for the number of Inches, of the equall or narrower side, in the right part and hanging Margin. At the common meeting where the one number answereth directly to the other, there your true Square shal appeare. This Square so found, shalbe referred to your Table of Timber measure: in the which pe may plainly see (if you runne downe by the left Margin, vntill your Inches square appear) how many Feete or Inches of your Ruler belong to a Foote square. As often as that measure there found, is contained in the Timber or Stone, so often and as many Feete square pe may conclude (without doubt) the piece of Timber or Stone to haue.

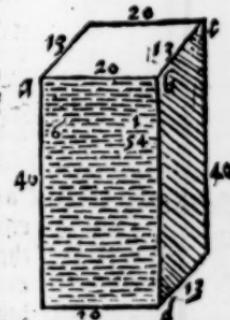
D

Ensample.

# The Art of measuring

## Ensample.

Suppose this squared Timber or Stone a. b. c. d. were to be measured, the broader side a. b. 20. Inches, & narrower side b. c. 13. Inches, the length 40. Inches. Now I must seek the broader side 20, in the upper Margine of the table. The narrower side 13, must be found in the right side and hanging Margine. At their common meeting, 16. Inches, and  $\frac{1}{4}$ . part of an Inch shall appear. This true square must be searched for in the table of timber measure. Wherefore looke for 16. in the Margine of this table. In the Squares with him rightward, ye shall finde 6. Inches, and  $\frac{1}{4}$ . which is three quarters of an Inch. Some deale lessle of your Ruler then 6. and  $\frac{1}{4}$ . layd out vpon the timber, maketh a Foote Square. And that measure so directly handled, is contained in the Length of your timber six times. Wherfore affirme six Foote there to bee, beside that is left  $\frac{1}{4}$ . part of a Foote. Note because the Squares at all times (in this Ensample) rile not to euuen Inches, but sometime to odde parts: therefore according to your discretion, adde or take away some part more or lessle in setting forth the Foote Square, as aboue is performed.



It were intolerable tediousnesse, yea impossible to set forth the true quantities of timber measure, to all odde Quantities of Squares. The discrete handling of these, the wittie shall bring to a sufficient exactnesse.

Of Timber or Stone; 3.5.10.20. or  
mo Sides Square. &c.

*The viij. Chapter.*

**W**hen Timber hath divers equal Squares in the head, and so through: first measure all the square sides round about the head or end of the Timber. Then take halfe the number of the whole measure for one breadth.

Then measure from the Center (which is the middle of the head, or end of the Timber) to the middest of the Square side, betweene the two Angles, and take the measure of that distance for the other breadth. Now resolt with the measures of these two breadths, (as before) to the Table of Squares: seeking the bigger number or breadth in the upper Margine, and the other lesser in the side Margine. With the square there found, haue recourse to the Table of Timber measure, and doe as I haue instructed.

*Ensample.*

Admit this small piece of Timber five square, c. f. g. h. Should be measured, every side being 12. Inches. If ye adde together in one summe all the five sides, they make 60. Inches. The halfe is 30: that serveth for one breadth. Then the Line c. f. which goeth from the Center or middest of the Square, to the middle of one side, is 8. Inches. The two numbers 30. and 8. must be sought (as before) in the table of squares following. At the common meeting, your square shall appeare 15. Inches,  $\frac{1}{2}$ . This square 15. seeke in the Table of Timber measure. There ye may see right with it 7. Inches, and  $\frac{1}{2}$ . Now because of  $\frac{1}{2}$ . the odde quantity of the

D. 2

Square:



## The Art of measuring

Square above 15 Inches, lay something lesse. Then see how oftentimes that measure (so with discretion handled) is from the one end of your Timber to the other: and assume so many times a Foote square there to be, as that measure is fould in the length of your Logge.

## How round and hollow Timber, Steeples, Pillars, Globes,&c. are to be measured.

The ix. Chapter.



**E**irst gird the Logge round about with some  
Line: then diuide the Line which compas-  
seth that timber into two equal parts: keepe  
the one part for the bigger breadth. After, ye  
shall diuide againe that whole length (the  
two and twenty part cast away) in three  
parts, and take the halfe of one of them for  
the other narrower breadth. With the measures of these two  
breadths, haste to your table, performing all things as afore is  
opened.

## Ensample.

Suppose this little piece of Timber, i.k.l.m. were to be measured, the compasses or girding 36. Inches, and the halfe of that is 18. being the one breadth: then the third of 36. is 12 : the halfe of it is 6. which is the other narrower breadth, with these two numbers 6. and 18. enter the Table of Squares following, and so the table of Timber measure. At the last (all things performed as before) ye shall finde in this round Logge, the length l. m. being 18. Inches, 1. Foote, and  $\frac{1}{2}$ . part of a foote. This is sufficient for all such like,



1

### A note of hollowed Timber.

If it chance that hollowed Timber be to be measured: measure the whole Logge as though it were not hollow, as above is declared. Then measure the narrower and broader side of the hollow, and see what is contained in that, as though it were massie Timber. Now pull out the content of it, from the whole above measured: the remaine of force must shew what Timber is included in that hollowed body.

I am vnable in few words to expresse to the unlearned, by what meane Pyramidal, or picked regular Steeples of all fashions are measured. Also how Pillers, how the content of Globes or Bowles are searched, vntille the Art of numbering were tasteth. That being knowne: thus (as now followeth) I teach.

### How the crassitude of picked Steeple is knowne.

Multiply the plaine of the Base in the third part of the Height: so yee haue the Crassitude. Or multiply the Content superficial (found as I haue instructed) in the Height of the Steeple, taking for your purpose the third part of that product.

### How the Content of Pillers is knowne.

Increase the Base plaine in his Altitude or Height: so haue Eye your desire.

# The Art of measuring

## How the Cubicall bodies of Globes are searched.

**T**he content Superficiall found, (as I haue opened) must be multiplied in the sixth part of the Diameter : the product is that ye require : Or the third part of the superficiall Content in halfe the Diameter. Or multiplye the plaine of the Circle in the whole Diameter : then take two third parts, which added, make the Crastitude.

### Of the halfe Circle.

**H**is Superficiall Content multiplied (as I said) bringeth the magnitude of him. If any man require ensamples of these last matters, or more sufficient handling : let them resort vnto my booke published of Geometrie, where they shall bee satisfied. These little appertaine to Carpenters or Masons : therefore not by ensample declared.

### A generall note.

**V**hen thou shalt bee put to measure some Body, without order or fashion, lacking part of his Squares, or having more then his Forme: if it lacke, thou shalt make it perfect, by obseruing diligently the running together of the sides. The parts wanting shall bee measured, as though they were there, which portions must be taken from the whole Body measured.

Also when there resulceth any moxe then the forme or Regular Square: first measure the square Body: then the Crastitude which aboundeth. All put together, doe shew the whole irregular Bodie. This sufficeth.

A Table to find the iust Radix or Square  
of any Timber or Stone.

**I**n the booueth you to know, that this table following is made for the true square of any maner timber: therefore understand that the numbers from 1. to 40. set aboue in the high Bargine, betoken the Inches of the broader side of the Timber. And the numbers from 1. and so downeward to 30. put in the right part and hanging Bargine of this table, signifie the inches of the narrower side: and to conclude brefly, the Element or figures set in every square roome, betoken the iust square. The bigger figures leftward in every square place, signifie the whole inches. And the other lesser righward in the same square diuided by a line, the parts of inches, as  $\frac{1}{2}$ . &c.

This first Fraction toward the left hand, betokeneth one halfe part of an inch: the other two fifts of an inch, and euerie figure or fraction having a point adiogned vnto him, some deale lese then that part is: as this part,  $\frac{1}{2}$  representeth scant halfe an inch, a very little quantity lese. And if it had two yicks by him, he shoulde haue declared some quantity more: as this other fraction or part,  $\frac{2}{5}$ : which is more then two fifts, a small deale.

It had not beeene needfull to haue put the parts of the Square so precisely as they are here: neither is it requisite so curiously to take them.

T A B U L A

| 1  | 2             | 3             | 4  | 5              | 6              | 7              | 8              | 9  | 10             | 11              | 12             | 13            | 14             | 15             | 16             | 17             | 18             | 19              | 20              | 21              | 22            |
|----|---------------|---------------|----|----------------|----------------|----------------|----------------|----|----------------|-----------------|----------------|---------------|----------------|----------------|----------------|----------------|----------------|-----------------|-----------------|-----------------|---------------|
| 1  | $\frac{3}{7}$ | $\frac{3}{4}$ | 2  | $\frac{5}{4}$  | $\frac{2}{3}$  | $\frac{2}{5}$  | $\frac{4}{3}$  | 3  | $\frac{1}{3}$  | $\frac{3}{2}$   | $\frac{2}{3}$  | $\frac{4}{3}$ | 3              | $\frac{7}{8}$  | 4              | $\frac{1}{8}$  | $\frac{1}{4}$  | $\frac{1}{4}$   | $\frac{1}{2}$   | $\frac{3}{4}$   |               |
| 2  | 2             | $\frac{2}{5}$ | 2  | $\frac{4}{5}$  | $\frac{1}{3}$  | $\frac{1}{2}$  | $\frac{3}{4}$  | 4  | $\frac{4}{3}$  | $\frac{2}{1}$   | $\frac{4}{3}$  | 5             | $\frac{1}{10}$ | $\frac{5}{4}$  | $\frac{2}{5}$  | $\frac{4}{5}$  | 6              | $\frac{6}{7}$   | $\frac{6}{3}$   | $\frac{6}{2}$   | $\frac{6}{3}$ |
| 3  | 3             | $\frac{3}{2}$ | 3  | $\frac{7}{4}$  | 4              | $\frac{4}{8}$  | $\frac{5}{5}$  | 5  | $\frac{3}{5}$  | $\frac{1}{2}$   | $\frac{5}{4}$  | 6             | 0              | $\frac{1}{4}$  | $\frac{5}{6}$  | $\frac{3}{2}$  | 7              | $\frac{1}{2}$   | $\frac{3}{2}$   | 7               | $\frac{3}{4}$ |
| 4  | 4             | $\frac{1}{2}$ | 5  | $\frac{1}{4}$  | $\frac{2}{3}$  | 6              | $\frac{1}{6}$  | 6  | $\frac{2}{3}$  | 7               | $\frac{1}{7}$  | 7             | $\frac{1}{2}$  | $\frac{7}{4}$  | 8              | $\frac{1}{8}$  | $\frac{1}{4}$  | 9               | $\frac{9}{10}$  | $\frac{9}{9}$   | $\frac{9}{8}$ |
| 5  | 5             | $\frac{1}{2}$ | 6  | $\frac{6}{9}$  | $\frac{1}{4}$  | $\frac{3}{7}$  | $\frac{1}{14}$ | 7  | $\frac{3}{5}$  | $\frac{8}{15}$  | $\frac{3}{16}$ | 8             | $\frac{3}{9}$  | $\frac{3}{5}$  | 9              | $\frac{2}{9}$  | $\frac{9}{10}$ | $\frac{10}{11}$ | $\frac{10}{10}$ | $\frac{10}{9}$  |               |
| 6  | 6             | $\frac{1}{2}$ | 7  | $\frac{7}{3}$  | $\frac{1}{7}$  | $\frac{3}{8}$  | $\frac{1}{14}$ | 8  | $\frac{1}{2}$  | $\frac{5}{6}$   | $\frac{1}{9}$  | 9             | $\frac{1}{2}$  | $\frac{7}{6}$  | $\frac{1}{10}$ | $\frac{4}{10}$ | $\frac{2}{10}$ | $\frac{2}{11}$  | $\frac{11}{11}$ | $\frac{11}{10}$ |               |
| 7  | 7             | $\frac{1}{2}$ | 8  | $\frac{8}{3}$  | $\frac{3}{8}$  | $\frac{4}{5}$  | $\frac{1}{15}$ | 9  | $\frac{1}{9}$  | $\frac{8}{9}$   | $\frac{1}{10}$ | 10            | $\frac{1}{10}$ | $\frac{5}{10}$ | $\frac{1}{10}$ | $\frac{9}{11}$ | $\frac{1}{11}$ | $\frac{11}{12}$ | $\frac{12}{12}$ | $\frac{12}{11}$ |               |
| 8  | 8             | $\frac{8}{2}$ | 9  | $\frac{9}{3}$  | $\frac{4}{9}$  | $\frac{1}{10}$ | $\frac{1}{10}$ | 11 | $\frac{1}{11}$ | $\frac{1}{11}$  | $\frac{2}{11}$ | 12            | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{4}{12}$ | $\frac{2}{12}$ | $\frac{2}{12}$  | $\frac{1}{13}$  | $\frac{1}{13}$  |               |
| 9  | 9             | $\frac{1}{2}$ | 10 | $\frac{10}{5}$ | $\frac{10}{5}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | 12 | $\frac{1}{11}$ | $\frac{12}{11}$ | $\frac{1}{12}$ | 13            | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{4}{13}$ | $\frac{2}{13}$ | $\frac{2}{13}$  | $\frac{1}{14}$  | $\frac{1}{14}$  |               |
| 10 | 10            | $\frac{1}{2}$ | 11 | $\frac{11}{5}$ | $\frac{11}{5}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | 13 | $\frac{1}{12}$ | $\frac{13}{12}$ | $\frac{1}{13}$ | 14            | $\frac{1}{13}$ | $\frac{1}{13}$ | $\frac{1}{13}$ | $\frac{4}{14}$ | $\frac{2}{14}$ | $\frac{2}{14}$  | $\frac{1}{15}$  | $\frac{1}{15}$  |               |
| 11 | 11            | $\frac{1}{2}$ | 12 | $\frac{12}{5}$ | $\frac{12}{5}$ | $\frac{1}{13}$ | $\frac{1}{13}$ | 14 | $\frac{1}{13}$ | $\frac{14}{13}$ | $\frac{1}{14}$ | 15            | $\frac{1}{14}$ | $\frac{1}{14}$ | $\frac{1}{14}$ | $\frac{4}{15}$ | $\frac{2}{15}$ | $\frac{2}{15}$  | $\frac{1}{16}$  | $\frac{1}{16}$  |               |
| 12 | 12            | $\frac{1}{2}$ | 13 | $\frac{13}{5}$ | $\frac{13}{5}$ | $\frac{1}{14}$ | $\frac{1}{14}$ | 15 | $\frac{1}{14}$ | $\frac{15}{14}$ | $\frac{1}{15}$ | 16            | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{4}{16}$ | $\frac{2}{16}$ | $\frac{2}{16}$  | $\frac{1}{17}$  | $\frac{1}{17}$  |               |
| 13 | 13            | $\frac{1}{2}$ | 14 | $\frac{14}{5}$ | $\frac{14}{5}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | 16 | $\frac{1}{15}$ | $\frac{16}{15}$ | $\frac{1}{16}$ | 17            | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{4}{17}$ | $\frac{2}{17}$ | $\frac{2}{17}$  | $\frac{1}{18}$  | $\frac{1}{18}$  |               |
| 14 | 14            | $\frac{1}{2}$ | 15 | $\frac{15}{5}$ | $\frac{15}{5}$ | $\frac{1}{17}$ | $\frac{1}{17}$ | 18 | $\frac{1}{17}$ | $\frac{18}{17}$ | $\frac{1}{18}$ | 19            | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{4}{19}$ | $\frac{2}{19}$ | $\frac{2}{19}$  | $\frac{1}{20}$  | $\frac{1}{20}$  |               |
| 15 | 15            | $\frac{1}{2}$ | 16 | $\frac{16}{5}$ | $\frac{16}{5}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | 17 | $\frac{1}{18}$ | $\frac{17}{18}$ | $\frac{1}{19}$ | 20            | $\frac{1}{19}$ | $\frac{1}{19}$ | $\frac{1}{19}$ | $\frac{4}{20}$ | $\frac{2}{20}$ | $\frac{2}{20}$  | $\frac{1}{21}$  | $\frac{1}{21}$  |               |
| 16 | 16            | $\frac{1}{2}$ | 17 | $\frac{17}{5}$ | $\frac{17}{5}$ | $\frac{1}{19}$ | $\frac{1}{19}$ | 21 | $\frac{1}{19}$ | $\frac{21}{19}$ | $\frac{1}{20}$ | 22            | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{4}{21}$ | $\frac{2}{21}$ | $\frac{2}{21}$  | $\frac{1}{22}$  | $\frac{1}{22}$  |               |
| 17 | 17            | $\frac{1}{2}$ | 18 | $\frac{18}{5}$ | $\frac{18}{5}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | 20 | $\frac{1}{21}$ | $\frac{20}{21}$ | $\frac{1}{22}$ | 21            | $\frac{1}{22}$ | $\frac{1}{22}$ | $\frac{1}{22}$ | $\frac{4}{23}$ | $\frac{2}{23}$ | $\frac{2}{23}$  | $\frac{1}{24}$  | $\frac{1}{24}$  |               |
| 18 | 18            | $\frac{1}{2}$ | 19 | $\frac{19}{5}$ | $\frac{19}{5}$ | $\frac{1}{22}$ | $\frac{1}{22}$ | 23 | $\frac{1}{22}$ | $\frac{23}{22}$ | $\frac{1}{24}$ | 24            | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{4}{25}$ | $\frac{2}{25}$ | $\frac{2}{25}$  | $\frac{1}{26}$  | $\frac{1}{26}$  |               |
| 19 | 19            | $\frac{1}{2}$ | 20 | $\frac{20}{5}$ | $\frac{20}{5}$ | $\frac{1}{23}$ | $\frac{1}{23}$ | 21 | $\frac{1}{23}$ | $\frac{21}{23}$ | $\frac{1}{24}$ | 22            | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{4}{25}$ | $\frac{2}{25}$ | $\frac{2}{25}$  | $\frac{1}{26}$  | $\frac{1}{26}$  |               |
| 20 | 20            | $\frac{1}{2}$ | 21 | $\frac{21}{5}$ | $\frac{21}{5}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | 22 | $\frac{1}{24}$ | $\frac{22}{24}$ | $\frac{1}{25}$ | 23            | $\frac{1}{25}$ | $\frac{1}{25}$ | $\frac{1}{25}$ | $\frac{4}{26}$ | $\frac{2}{26}$ | $\frac{2}{26}$  | $\frac{1}{27}$  | $\frac{1}{27}$  |               |
| 21 | 21            | $\frac{1}{2}$ | 22 | $\frac{22}{5}$ | $\frac{22}{5}$ | $\frac{1}{25}$ | $\frac{1}{25}$ | 23 | $\frac{1}{25}$ | $\frac{23}{25}$ | $\frac{1}{26}$ | 24            | $\frac{1}{26}$ | $\frac{1}{26}$ | $\frac{1}{26}$ | $\frac{4}{27}$ | $\frac{2}{27}$ | $\frac{2}{27}$  | $\frac{1}{28}$  | $\frac{1}{28}$  |               |

The Table  
of Squares

Place this Table before D. and E.

# R A D I C V M

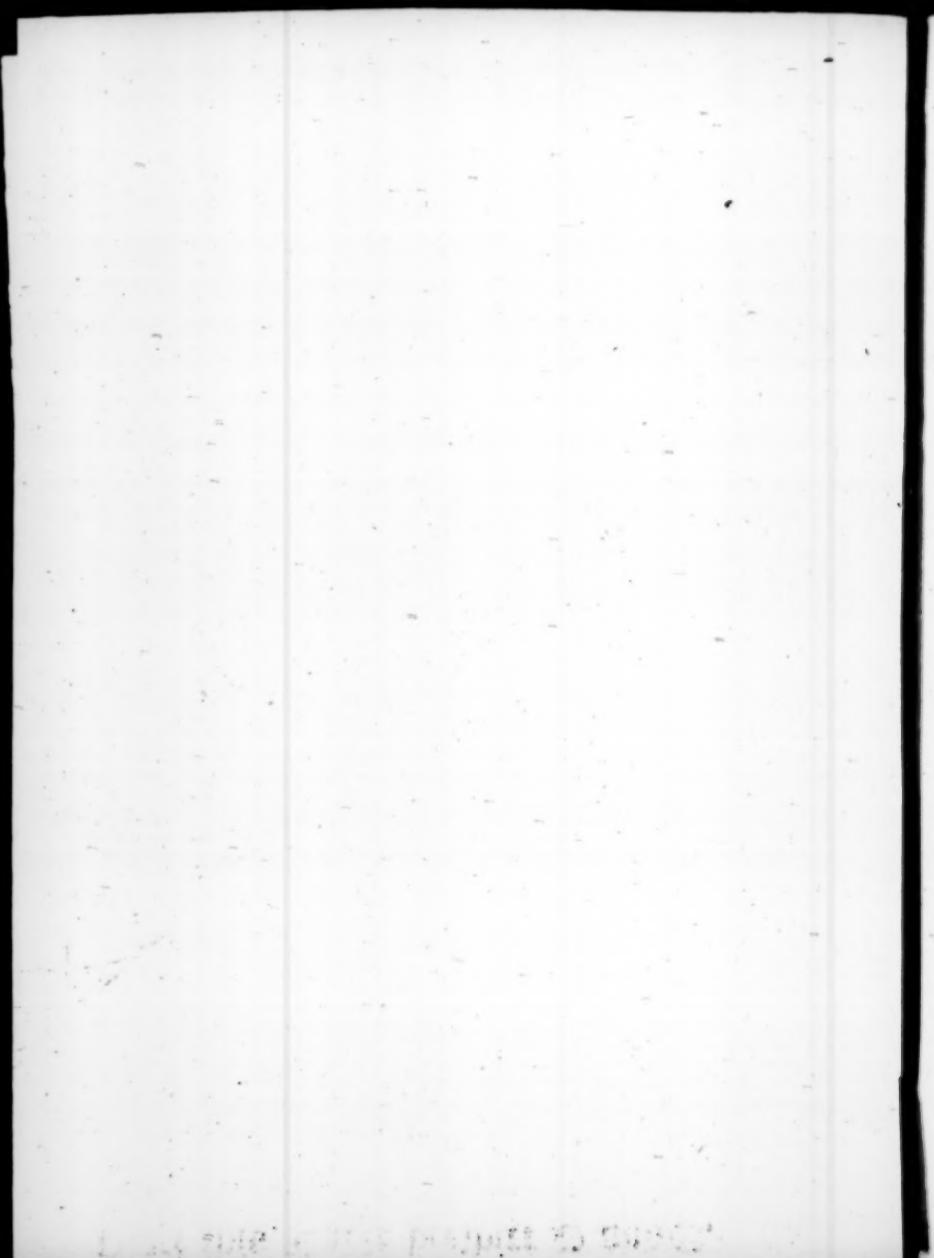
| 21                | 22                | 23                | 24                | 25                | 26                | 27                | 28                | 29                | 30                  | 31                | 32                | 33                | 34                | 35                | 36                | 37                | 38                | 39                | 40              |
|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|---------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-----------------|
| 4 $\frac{1}{5}$   | 4 $\frac{6}{5}$   | 4 $\frac{3}{4}$   | 5 -               | 5                 | 5 $\frac{1}{10}$  | 5 $\frac{3}{10}$  | 5 $\frac{1}{3}$   | 5 $\frac{2}{5}$   | 5 $\frac{1}{2}$     | 5 $\frac{1}{3}$   | 5 $\frac{1}{4}$   | 5 $\frac{1}{5}$   | 5 $\frac{1}{6}$   | 5 $\frac{1}{7}$   | 5 $\frac{1}{8}$   | 6                 | 6 $\frac{1}{10}$  | 6 $\frac{1}{9}$   | 6 $\frac{1}{8}$ |
| 6 $\frac{1}{2}$   | 6 $\frac{2}{3}$   | 6 $\frac{5}{3}$   | 7 -               | 7 $\frac{1}{6}$   | 7 $\frac{3}{4}$   | 7 $\frac{2}{3}$   | 7 $\frac{1}{2}$   | 7 $\frac{3}{5}$   | 7 $\frac{2}{3}$     | 7 $\frac{1}{2}$   | 7 $\frac{3}{8}$   | 7 $\frac{1}{6}$   | 7 $\frac{3}{8}$   | 7 $\frac{1}{6}$   | 8                 | 8 $\frac{1}{8}$   | 8 $\frac{1}{7}$   | 8 $\frac{1}{6}$   |                 |
| 8 -               | 8 $\frac{1}{8}$   | 8 $\frac{5}{4}$   | 8 $\frac{7}{2}$   | 8 $\frac{2}{3}$   | 8 $\frac{7}{6}$   | 9 -               | 9 $\frac{1}{6}$   | 9 $\frac{2}{3}$   | 9 $\frac{4}{5}$     | 10 -              | 10 $\frac{2}{5}$  | 10 $\frac{4}{5}$  | 10 $\frac{1}{5}$  | 10 $\frac{2}{3}$  | 10 $\frac{1}{2}$  | 10 $\frac{2}{7}$  | 10 $\frac{9}{7}$  | 10 $\frac{9}{4}$  | 10 -            |
| 9 $\frac{1}{2}$   | 9 $\frac{3}{2}$   | 9 $\frac{9}{4}$   | 10 -              | 10 $\frac{4}{5}$  | 10 $\frac{2}{5}$  | 10 $\frac{1}{5}$  | 11 -              | 11 $\frac{1}{8}$  | 11 $\frac{1}{7}$    | 11 $\frac{1}{6}$  | 11 $\frac{3}{5}$  | 11 $\frac{1}{5}$  | 11 $\frac{3}{4}$  | 11 $\frac{1}{3}$  | 12                | 12 $\frac{1}{6}$  | 12 $\frac{1}{5}$  | 12 $\frac{1}{4}$  |                 |
| 10 $\frac{1}{10}$ | 10 $\frac{3}{2}$  | 10 $\frac{3}{4}$  | 11 -              | 11 $\frac{1}{6}$  | 11 $\frac{2}{3}$  | 11 $\frac{1}{2}$  | 12 $\frac{1}{4}$  | 12 $\frac{1}{3}$  | 12 $\frac{1}{2}$    | 12 $\frac{1}{1}$  | 12 $\frac{1}{3}$  | 12 $\frac{1}{2}$  | 12 $\frac{1}{1}$  | 13                | 13 $\frac{3}{5}$  | 13 $\frac{2}{3}$  | 13 $\frac{1}{2}$  | 13 -              |                 |
| 11 -              | 11 $\frac{1}{2}$  | 11 $\frac{3}{4}$  | 12 -              | 12 $\frac{1}{4}$  | 12 $\frac{1}{2}$  | 12 $\frac{1}{3}$  | 13 -              | 13 $\frac{1}{8}$  | 13 $\frac{1}{7}$    | 13 $\frac{1}{6}$  | 14 $\frac{1}{4}$  | 14 $\frac{1}{3}$  | 14 $\frac{1}{2}$  | 14 $\frac{1}{1}$  | 15                | 15 $\frac{2}{5}$  | 15 $\frac{1}{4}$  | 15 $\frac{1}{3}$  | 15 -            |
| 12 -              | 12 $\frac{1}{12}$ | 12 $\frac{2}{3}$  | 13 -              | 13 $\frac{1}{4}$  | 13 $\frac{3}{2}$  | 13 $\frac{3}{4}$  | 14 -              | 14 $\frac{1}{2}$  | 14 $\frac{1}{1}$    | 15 -              | 15 $\frac{3}{5}$  | 15 $\frac{2}{5}$  | 15 $\frac{1}{5}$  | 15 $\frac{1}{7}$  | 16                | 16 $\frac{1}{3}$  | 16 $\frac{1}{2}$  | 16 $\frac{1}{3}$  | 16 -            |
| 17 -              | 13 $\frac{1}{4}$  | 13 $\frac{4}{2}$  | 13 -              | 13 $\frac{1}{6}$  | 14 $\frac{2}{3}$  | 14 $\frac{1}{3}$  | 15 -              | 15 $\frac{1}{5}$  | 15 $\frac{1}{4}$    | 16 -              | 16 $\frac{1}{4}$  | 16 $\frac{1}{3}$  | 16 $\frac{1}{2}$  | 16 $\frac{1}{1}$  | 17                | 17 $\frac{1}{5}$  | 17 $\frac{2}{3}$  | 17 $\frac{1}{2}$  | 17 -            |
| 13 $\frac{1}{4}$  | 14 $\frac{1}{4}$  | 14 $\frac{1}{3}$  | 14 $\frac{1}{2}$  | 15 $\frac{1}{5}$  | 15 $\frac{2}{3}$  | 15 $\frac{1}{6}$  | 16 -              | 16 $\frac{1}{4}$  | 16 $\frac{1}{3}$    | 16 $\frac{1}{2}$  | 16 $\frac{1}{1}$  | 17 -              | 17 $\frac{1}{4}$  | 17 $\frac{1}{3}$  | 18                | 18 $\frac{1}{4}$  | 18 $\frac{1}{3}$  | 18 $\frac{1}{2}$  | 18 -            |
| 14 $\frac{1}{4}$  | 14 $\frac{1}{5}$  | 14 $\frac{1}{6}$  | 15 $\frac{1}{7}$  | 15 $\frac{2}{5}$  | 15 $\frac{1}{8}$  | 16 -              | 16 $\frac{1}{6}$  | 16 $\frac{1}{5}$  | 16 $\frac{1}{4}$    | 17 -              | 17 $\frac{1}{7}$  | 17 $\frac{1}{6}$  | 17 $\frac{1}{5}$  | 17 $\frac{1}{4}$  | 18                | 18 $\frac{1}{3}$  | 18 $\frac{1}{2}$  | 18 $\frac{1}{1}$  | 18 -            |
| 14 $\frac{1}{2}$  | 14 $\frac{1}{5}$  | 15 $\frac{1}{6}$  | 15 $\frac{2}{3}$  | 15 $\frac{1}{5}$  | 16 $\frac{1}{8}$  | 16 $\frac{2}{5}$  | 15 $\frac{1}{4}$  | 17 -              | 17 $\frac{1}{5}$    | 17 $\frac{1}{4}$  | 17 $\frac{1}{3}$  | 18 -              | 18 $\frac{1}{6}$  | 18 $\frac{1}{5}$  | 19                | 19 $\frac{1}{2}$  | 19 $\frac{1}{1}$  | 19 -              | 20              |
| 15 $\frac{1}{3}$  | 15 $\frac{1}{5}$  | 15 $\frac{1}{6}$  | 16 $\frac{1}{8}$  | 16 $\frac{1}{6}$  | 16 $\frac{1}{5}$  | 16 $\frac{1}{4}$  | 17 -              | 17 $\frac{1}{7}$  | 17 $\frac{1}{6}$    | 17 $\frac{1}{5}$  | 18 -              | 18 $\frac{1}{8}$  | 18 $\frac{1}{7}$  | 19 -              | 19 $\frac{1}{6}$  | 20 $\frac{1}{5}$  | 20 $\frac{1}{4}$  | 21 -              |                 |
| 15 $\frac{1}{6}$  | 16 $\frac{1}{7}$  | 16 $\frac{1}{8}$  | 17 $\frac{1}{9}$  | 17 $\frac{1}{8}$  | 17 $\frac{1}{7}$  | 17 $\frac{1}{6}$  | 18 -              | 18 $\frac{1}{9}$  | 18 $\frac{1}{8}$    | 18 $\frac{1}{7}$  | 19 -              | 19 $\frac{1}{10}$ | 19 $\frac{1}{9}$  | 19 $\frac{1}{8}$  | 20                | 20 $\frac{1}{7}$  | 20 $\frac{1}{6}$  | 20 $\frac{1}{5}$  | 21 -            |
| 16 $\frac{1}{16}$ | 16 $\frac{1}{15}$ | 16 $\frac{1}{17}$ | 17 $\frac{1}{18}$ | 17 $\frac{1}{17}$ | 17 $\frac{1}{16}$ | 18 -              | 18 $\frac{1}{19}$ | 18 $\frac{1}{18}$ | 18 $\frac{1}{17}$   | 19 -              | 19 $\frac{1}{20}$ | 19 $\frac{1}{19}$ | 19 $\frac{1}{18}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -              | 21 $\frac{1}{22}$ |                 |
| 16 $\frac{1}{21}$ | 17 $\frac{1}{17}$ | 17 $\frac{1}{18}$ | 17 $\frac{1}{19}$ | 17 $\frac{1}{18}$ | 17 $\frac{1}{17}$ | 18 -              | 18 $\frac{1}{19}$ | 18 $\frac{1}{18}$ | 18 $\frac{1}{17}$   | 19 -              | 19 $\frac{1}{20}$ | 19 $\frac{1}{19}$ | 19 $\frac{1}{18}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -              | 21 $\frac{1}{22}$ |                 |
| 17 $\frac{1}{17}$ | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{19}$ | 18 $\frac{1}{20}$ | 19 -              | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 19 $\frac{1}{19}$ | 20 -                | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -              | 21 $\frac{1}{22}$ | 21 $\frac{1}{21}$ | 22 -              | 22 $\frac{1}{23}$ | 22 $\frac{1}{22}$ | 22 $\frac{1}{21}$ | 22 -            |
| 17 $\frac{1}{17}$ | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{19}$ | 18 $\frac{1}{20}$ | 19 -              | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 19 $\frac{1}{19}$ | 20 -                | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -              | 21 $\frac{1}{22}$ | 21 $\frac{1}{21}$ | 22 -              | 22 $\frac{1}{23}$ | 22 $\frac{1}{22}$ | 22 $\frac{1}{21}$ | 22 -            |
| 17 $\frac{1}{18}$ | 18 $\frac{1}{19}$ | 18 -              | 19 $\frac{1}{20}$ | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -                | 21 $\frac{1}{22}$ | 21 $\frac{1}{21}$ | 22 -              | 22 $\frac{1}{23}$ | 22 $\frac{1}{22}$ | 23 -              | 23 $\frac{1}{24}$ | 23 $\frac{1}{23}$ | 23 $\frac{1}{22}$ | 23 -            |
| 18 $\frac{1}{18}$ | 18 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{20}$ | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{20}$ | 21 -                | 21 $\frac{1}{22}$ | 21 $\frac{1}{21}$ | 22 -              | 22 $\frac{1}{23}$ | 22 $\frac{1}{22}$ | 23 -              | 23 $\frac{1}{24}$ | 23 $\frac{1}{23}$ | 23 $\frac{1}{22}$ | 23 -            |
| 18 $\frac{1}{19}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{22}$ | 21 -              | 21 $\frac{1}{23}$ | 21 $\frac{1}{22}$ | 22 -              | 22 $\frac{1}{23}$   | 22 $\frac{1}{22}$ | 23 -              | 23 $\frac{1}{24}$ | 23 $\frac{1}{23}$ | 24 -              | 24 $\frac{1}{25}$ | 24 $\frac{1}{24}$ | 25 -              | 25 $\frac{1}{26}$ |                 |
| 8 $\frac{1}{8}$   | 19 $\frac{1}{9}$  | 9 -               | 10 $\frac{1}{11}$ | 10 $\frac{1}{12}$ | 11 -              | 11 $\frac{1}{13}$ | 11 $\frac{1}{12}$ | 12 -              | 12 $\frac{1}{13}$   | 12 $\frac{1}{12}$ | 13 -              | 13 $\frac{1}{14}$ | 13 $\frac{1}{13}$ | 14 -              | 14 $\frac{1}{15}$ | 14 $\frac{1}{14}$ | 15 -              | 15 $\frac{1}{16}$ |                 |
| 8 $\frac{1}{9}$   | 19 $\frac{1}{10}$ | 10 -              | 10 $\frac{1}{11}$ | 10 $\frac{1}{12}$ | 11 -              | 11 $\frac{1}{13}$ | 11 $\frac{1}{12}$ | 12 -              | 12 $\frac{1}{13}$   | 12 $\frac{1}{12}$ | 13 -              | 13 $\frac{1}{14}$ | 13 $\frac{1}{13}$ | 14 -              | 14 $\frac{1}{15}$ | 14 $\frac{1}{14}$ | 15 -              | 15 $\frac{1}{16}$ |                 |
| 8 $\frac{1}{10}$  | 19 $\frac{1}{11}$ | 11 -              | 11 $\frac{1}{12}$ | 11 $\frac{1}{13}$ | 12 -              | 12 $\frac{1}{14}$ | 12 $\frac{1}{13}$ | 13 -              | 13 $\frac{1}{15}$   | 13 $\frac{1}{14}$ | 14 -              | 14 $\frac{1}{16}$ | 14 $\frac{1}{15}$ | 15 -              | 15 $\frac{1}{17}$ | 15 $\frac{1}{16}$ | 16 -              | 16 $\frac{1}{18}$ |                 |
| 8 $\frac{1}{11}$  | 19 $\frac{1}{12}$ | 12 -              | 12 $\frac{1}{13}$ | 12 $\frac{1}{14}$ | 13 -              | 13 $\frac{1}{15}$ | 13 $\frac{1}{14}$ | 14 -              | 14 $\frac{1}{16}$   | 14 $\frac{1}{15}$ | 15 -              | 15 $\frac{1}{17}$ | 15 $\frac{1}{16}$ | 16 -              | 16 $\frac{1}{18}$ | 16 $\frac{1}{17}$ | 17 -              | 17 $\frac{1}{19}$ |                 |
| 8 $\frac{1}{12}$  | 19 $\frac{1}{13}$ | 13 -              | 13 $\frac{1}{14}$ | 13 $\frac{1}{15}$ | 14 -              | 14 $\frac{1}{16}$ | 14 $\frac{1}{15}$ | 15 -              | 15 $\frac{1}{17}$   | 15 $\frac{1}{16}$ | 16 -              | 16 $\frac{1}{18}$ | 16 $\frac{1}{17}$ | 17 -              | 17 $\frac{1}{19}$ | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{20}$ |                 |
| 8 $\frac{1}{13}$  | 19 $\frac{1}{14}$ | 14 -              | 14 $\frac{1}{15}$ | 14 $\frac{1}{16}$ | 15 -              | 15 $\frac{1}{17}$ | 15 $\frac{1}{16}$ | 16 -              | 16 $\frac{1}{18}$   | 16 $\frac{1}{17}$ | 17 -              | 17 $\frac{1}{19}$ | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{20}$ | 18 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{21}$ |                 |
| 8 $\frac{1}{14}$  | 19 $\frac{1}{15}$ | 15 -              | 15 $\frac{1}{16}$ | 15 $\frac{1}{17}$ | 16 -              | 16 $\frac{1}{18}$ | 16 $\frac{1}{17}$ | 17 -              | 17 $\frac{1}{19}$   | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{20}$ | 18 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{22}$ |                 |
| 8 $\frac{1}{15}$  | 19 $\frac{1}{16}$ | 16 -              | 16 $\frac{1}{17}$ | 16 $\frac{1}{18}$ | 17 -              | 17 $\frac{1}{19}$ | 17 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{20}$   | 18 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{22}$ | 20 $\frac{1}{21}$ | 21 -              | 21 $\frac{1}{23}$ |                 |
| 8 $\frac{1}{16}$  | 19 $\frac{1}{17}$ | 17 -              | 17 $\frac{1}{18}$ | 17 $\frac{1}{19}$ | 18 -              | 18 $\frac{1}{20}$ | 18 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{21}$   | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{22}$ | 20 $\frac{1}{21}$ | 21 -              | 21 $\frac{1}{23}$ | 21 $\frac{1}{22}$ | 22 -              | 22 $\frac{1}{24}$ |                 |
| 8 $\frac{1}{17}$  | 19 $\frac{1}{18}$ | 18 -              | 18 $\frac{1}{19}$ | 18 $\frac{1}{20}$ | 19 -              | 19 $\frac{1}{21}$ | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{21}$   | 20 $\frac{1}{20}$ | 21 -              | 21 $\frac{1}{22}$ | 21 $\frac{1}{21}$ | 22 -              | 22 $\frac{1}{23}$ | 22 $\frac{1}{22}$ | 23 -              | 23 $\frac{1}{24}$ |                 |
| 8 $\frac{1}{18}$  | 19 $\frac{1}{19}$ | 19 -              | 19 $\frac{1}{20}$ | 19 $\frac{1}{21}$ | 20 -              | 20 $\frac{1}{22}$ | 20 $\frac{1}{21}$ | 21 -              | 21 $\frac{1}{23}$   | 21 $\frac{1}{22}$ | 22 -              | 22 $\frac{1}{24}$ | 22 $\frac{1}{23}$ | 23 -              | 23 $\frac{1}{25}$ | 23 $\frac{1}{24}$ | 24 -              | 24 $\frac{1}{26}$ |                 |
| 8 $\frac{1}{19}$  | 19 $\frac{1}{20}$ | 20 -              | 20 $\frac{1}{21}$ | 20 $\frac{1}{22}$ | 21 -              | 21 $\frac{1}{23}$ | 21 $\frac{1}{22}$ | 22 -              | 22 $\frac{1}{24}$   | 22 $\frac{1}{23}$ | 23 -              | 23 $\frac{1}{25}$ | 23 $\frac{1}{24}$ | 24 -              | 24 $\frac{1}{26}$ | 24 $\frac{1}{25}$ | 25 -              | 25 $\frac{1}{27}$ |                 |
| 8 $\frac{1}{20}$  | 20 $\frac{1}{21}$ | 21 -              | 21 $\frac{1}{22}$ | 21 $\frac{1}{23}$ | 22 -              | 22 $\frac{1}{24}$ | 22 $\frac{1}{23}$ | 23 -              | 23 $\frac{1}{25}$   | 23 $\frac{1}{24}$ | 24 -              | 24 $\frac{1}{26}$ | 24 $\frac{1}{25}$ | 25 -              | 25 $\frac{1}{27}$ | 25 $\frac{1}{26}$ | 26 -              | 26 $\frac{1}{28}$ |                 |
| 8 $\frac{1}{21}$  | 20 $\frac{1}{22}$ | 21 -              | 21 $\frac{1}{23}$ | 21 $\frac{1}{24}$ | 22 -              | 22 $\frac{1}{25}$ | 22 $\frac{1}{24}$ | 23 -              | 23 $\frac{1}{26}$   | 23 $\frac{1}{25}$ | 24 -              | 24 $\frac{1}{27}$ | 24 $\frac{1}{26}$ | 25 -              | 25 $\frac{1}{28}$ | 25 $\frac{1}{27}$ | 26 -              | 26 $\frac{1}{29}$ |                 |
| 8 $\frac{1}{22}$  | 20 $\frac{1}{23}$ | 21 -              | 21 $\frac{1}{24}$ | 21 $\frac{1}{25}$ | 22 -              | 22 $\frac{1}{26}$ | 22 $\frac{1}{25}$ | 23 -              | 23 $\frac{1}{27}$   | 23 $\frac{1}{26}$ | 24 -              | 24 $\frac{1}{28}$ | 24 $\frac{1}{27}$ | 25 -              | 25 $\frac{1}{29}$ | 25 $\frac{1}{28}$ | 26 -              | 26 $\frac{1}{30}$ |                 |
| 8 $\frac{1}{23}$  | 20 $\frac{1}{24}$ | 21 -              | 21 $\frac{1}{25}$ | 21 $\frac{1}{26}$ | 22 -              | 22 $\frac{1}{27}$ | 22 $\frac{1}{26}$ | 23 -              | 23 $\frac{1}{28}$   | 23 $\frac{1}{27}$ | 24 -              | 24 $\frac{1}{29}$ | 24 $\frac{1}{28}$ | 25 -              | 25 $\frac{1}{30}$ | 25 $\frac{1}{29}$ | 26 -              | 26 $\frac{1}{31}$ |                 |
| 8 $\frac{1}{24}$  | 20 $\frac{1}{25}$ | 21 -              | 21 $\frac{1}{26}$ | 21 $\frac{1}{27}$ | 22 -              | 22 $\frac{1}{28}$ | 22 $\frac{1}{27}$ | 23 -              | 23 $\frac{1}{29}$   | 23 $\frac{1}{28}$ | 24 -              | 24 $\frac{1}{30}$ | 24 $\frac{1}{29}$ | 25 -              | 25 $\frac{1}{31}$ | 25 $\frac{1}{30}$ | 26 -              | 26 $\frac{1}{32}$ |                 |
| 8 $\frac{1}{25}$  | 20 $\frac{1}{26}$ | 21 -              | 21 $\frac{1}{27}$ | 21 $\frac{1}{28}$ | 22 -              | 22 $\frac{1}{29}$ | 22 $\frac{1}{28}$ | 23 -              | 23 $\frac{1}{30}$   | 23 $\frac{1}{29}$ | 24 -              | 24 $\frac{1}{31}$ | 24 $\frac{1}{30}$ | 25 -              | 25 $\frac{1}{32}$ | 25 $\frac{1}{31}$ | 26 -              | 26 $\frac{1}{33}$ |                 |
| 8 $\frac{1}{26}$  | 20 $\frac{1}{27}$ | 21 -              | 21 $\frac{1}{28}$ | 21 $\frac{1}{29}$ | 22 -              | 22 $\frac{1}{30}$ | 22 $\frac{1}{29}$ | 23 -              | 23 $\frac{1}{31}$   | 23 $\frac{1}{30}$ | 24 -              | 24 $\frac{1}{32}$ | 24 $\frac{1}{31}$ | 25 -              | 25 $\frac{1}{33}$ | 25 $\frac{1}{32}$ | 26 -              | 26 $\frac{1}{34}$ |                 |
| 8 $\frac{1}{27}$  | 20 $\frac{1}{28}$ | 21 -              | 21 $\frac{1}{29}$ | 21 $\frac{1}{30}$ | 22 -              | 22 $\frac{1}{31}$ | 22 $\frac{1}{30}$ | 23 -              | 23 $\frac{1}{32}$   | 23 $\frac{1}{31}$ | 24 -              | 24 $\frac{1}{33}$ | 24 $\frac{1}{32}$ | 25 -              | 25 $\frac{1}{34}$ | 25 $\frac{1}{33}$ | 26 -              | 26 $\frac{1}{35}$ |                 |
| 8 $\frac{1}{28}$  | 20 $\frac{1}{29}$ | 21 -              | 21 $\frac{1}{30}$ | 21 $\frac{1}{31}$ | 22 -              | 22 $\frac{1}{32}$ | 22 $\frac{1}{31}$ | 23 -              | 23 $\frac{1}{33}</$ |                   |                   |                   |                   |                   |                   |                   |                   |                   |                 |

| 1  | 2              | 3              | 4              | 5              | 6              | 7             | 8              | 9              | 10              | 11             | 12              | 13              | 14             | 15              | 16              | 17              | 18              | 19             | 20              | 21              | 22 |
|----|----------------|----------------|----------------|----------------|----------------|---------------|----------------|----------------|-----------------|----------------|-----------------|-----------------|----------------|-----------------|-----------------|-----------------|-----------------|----------------|-----------------|-----------------|----|
| 1  | $\frac{3}{7}$  | $\frac{3}{4}$  | 2              | $\frac{5}{4}$  | $\frac{2}{3}$  | $\frac{2}{5}$ | $\frac{4}{3}$  | 3              | $\frac{1}{2}$   | $\frac{3}{2}$  | $\frac{4}{3}$   | $\frac{3}{4}$   | $\frac{7}{8}$  | 4               | $\frac{4}{8}$   | $\frac{4}{4}$   | $\frac{4}{3}$   | $\frac{4}{2}$  | $\frac{3}{4}$   | $\frac{6}{9}$   |    |
| 2  | $\frac{2}{5}$  | $\frac{2}{3}$  | $\frac{1}{3}$  | $\frac{1}{2}$  | $\frac{3}{4}$  | $\frac{4}{5}$ | $\frac{4}{3}$  | $\frac{4}{2}$  | $\frac{5}{3}$   | $\frac{5}{6}$  | $\frac{4}{5}$   | $\frac{5}{4}$   | $\frac{2}{3}$  | $\frac{5}{6}$   | $\frac{4}{5}$   | $\frac{6}{5}$   | $\frac{6}{3}$   | $\frac{6}{2}$  | $\frac{6}{3}$   | $\frac{2}{3}$   |    |
| 3  | $\frac{3}{2}$  | $\frac{6}{5}$  | $\frac{1}{4}$  | $\frac{4}{3}$  | $\frac{5}{8}$  | $\frac{5}{3}$ | $\frac{2}{5}$  | $\frac{3}{4}$  | $\frac{6}{5}$   | $\frac{2}{3}$  | $\frac{5}{6}$   | $\frac{3}{5}$   | $\frac{7}{8}$  | 7               | $\frac{7}{8}$   | $\frac{7}{7}$   | $\frac{7}{6}$   | $\frac{7}{5}$  | $\frac{7}{4}$   | $\frac{8}{9}$   |    |
| 4  | $\frac{4}{2}$  | $\frac{5}{3}$  | $\frac{1}{4}$  | $\frac{5}{3}$  | $\frac{2}{6}$  | $\frac{6}{5}$ | $\frac{4}{3}$  | $\frac{6}{2}$  | $\frac{7}{3}$   | $\frac{7}{5}$  | $\frac{4}{3}$   | $\frac{7}{2}$   | $\frac{3}{4}$  | $\frac{8}{7}$   | $\frac{4}{3}$   | $\frac{9}{8}$   | $\frac{9}{7}$   | $\frac{9}{6}$  | $\frac{9}{5}$   | $\frac{9}{4}$   |    |
| 5  | $\frac{5}{2}$  | $\frac{6}{5}$  | $\frac{6}{7}$  | $\frac{6}{4}$  | $\frac{7}{4}$  | $\frac{1}{2}$ | $\frac{7}{3}$  | $\frac{7}{4}$  | $\frac{8}{5}$   | $\frac{2}{3}$  | $\frac{8}{9}$   | $\frac{3}{5}$   | $\frac{9}{7}$  | $\frac{2}{5}$   | $\frac{9}{2}$   | $\frac{7}{5}$   | $\frac{10}{9}$  | $\frac{10}{8}$ | $\frac{10}{7}$  | $\frac{10}{6}$  |    |
| 6  | $\frac{6}{2}$  | $\frac{7}{5}$  | $\frac{7}{3}$  | $\frac{7}{4}$  | $\frac{8}{3}$  | $\frac{1}{2}$ | $\frac{8}{2}$  | $\frac{3}{5}$  | $\frac{9}{6}$   | $\frac{9}{2}$  | $\frac{7}{6}$   | $\frac{10}{9}$  | $\frac{10}{7}$ | $\frac{10}{5}$  | $\frac{10}{3}$  | $\frac{11}{11}$ | $\frac{11}{10}$ | $\frac{11}{9}$ | $\frac{11}{8}$  | $\frac{11}{7}$  |    |
| 7  | $\frac{7}{2}$  | $\frac{8}{5}$  | $\frac{8}{3}$  | $\frac{8}{5}$  | $\frac{9}{5}$  | $\frac{2}{3}$ | $\frac{9}{6}$  | $\frac{9}{5}$  | $\frac{10}{9}$  | $\frac{10}{7}$ | $\frac{10}{5}$  | $\frac{10}{11}$ | $\frac{10}{9}$ | $\frac{11}{11}$ | $\frac{11}{10}$ | $\frac{11}{9}$  | $\frac{11}{8}$  | $\frac{11}{7}$ | $\frac{12}{11}$ | $\frac{12}{10}$ |    |
| 8  | $\frac{8}{2}$  | $\frac{9}{5}$  | $\frac{9}{3}$  | $\frac{9}{5}$  | $\frac{10}{5}$ | $\frac{1}{2}$ | $\frac{11}{5}$ | $\frac{11}{3}$ | $\frac{11}{5}$  | $\frac{11}{3}$ | $\frac{11}{5}$  | $\frac{12}{5}$  | $\frac{12}{3}$ | $\frac{12}{5}$  | $\frac{12}{3}$  | $\frac{12}{5}$  | $\frac{12}{3}$  | $\frac{12}{5}$ | $\frac{12}{3}$  | $\frac{13}{4}$  |    |
| 9  | $\frac{9}{2}$  | $\frac{10}{5}$ | $\frac{10}{3}$ | $\frac{10}{5}$ | $\frac{11}{5}$ | $\frac{1}{2}$ | $\frac{12}{5}$ | $\frac{11}{3}$ | $\frac{12}{5}$  | $\frac{12}{3}$ | $\frac{12}{5}$  | $\frac{12}{3}$  | $\frac{13}{5}$ | $\frac{13}{3}$  | $\frac{13}{5}$  | $\frac{13}{3}$  | $\frac{13}{5}$  | $\frac{13}{4}$ | $\frac{13}{5}$  | $\frac{13}{4}$  |    |
| 10 | $\frac{10}{2}$ | $\frac{11}{5}$ | $\frac{11}{3}$ | $\frac{11}{5}$ | $\frac{12}{5}$ | $\frac{3}{4}$ | $\frac{12}{4}$ | $\frac{11}{5}$ | $\frac{13}{3}$  | $\frac{13}{5}$ | $\frac{13}{3}$  | $\frac{13}{5}$  | $\frac{14}{3}$ | $\frac{14}{5}$  | $\frac{14}{3}$  | $\frac{14}{5}$  | $\frac{14}{3}$  | $\frac{14}{5}$ | $\frac{14}{3}$  | $\frac{14}{5}$  |    |
| 11 | $\frac{11}{2}$ | $\frac{12}{5}$ | $\frac{12}{3}$ | $\frac{12}{5}$ | $\frac{13}{5}$ | $\frac{1}{2}$ | $\frac{12}{4}$ | $\frac{12}{3}$ | $\frac{13}{4}$  | $\frac{13}{3}$ | $\frac{13}{4}$  | $\frac{13}{3}$  | $\frac{14}{3}$ | $\frac{14}{2}$  | $\frac{14}{3}$  | $\frac{14}{2}$  | $\frac{14}{3}$  | $\frac{14}{5}$ | $\frac{15}{3}$  | $\frac{15}{2}$  |    |
| 12 | $\frac{12}{2}$ | $\frac{13}{5}$ | $\frac{13}{3}$ | $\frac{13}{5}$ | $\frac{14}{5}$ | $\frac{2}{3}$ | $\frac{13}{4}$ | $\frac{13}{3}$ | $\frac{14}{3}$  | $\frac{14}{2}$ | $\frac{14}{3}$  | $\frac{14}{2}$  | $\frac{15}{3}$ | $\frac{15}{2}$  | $\frac{15}{3}$  | $\frac{15}{2}$  | $\frac{15}{3}$  | $\frac{16}{5}$ | $\frac{16}{3}$  | $\frac{16}{5}$  |    |
| 13 | $\frac{13}{2}$ | $\frac{14}{5}$ | $\frac{14}{3}$ | $\frac{14}{5}$ | $\frac{15}{5}$ | $\frac{1}{2}$ | $\frac{14}{4}$ | $\frac{14}{3}$ | $\frac{15}{4}$  | $\frac{15}{3}$ | $\frac{15}{4}$  | $\frac{15}{3}$  | $\frac{16}{3}$ | $\frac{16}{2}$  | $\frac{16}{3}$  | $\frac{16}{2}$  | $\frac{16}{3}$  | $\frac{16}{5}$ | $\frac{17}{3}$  | $\frac{17}{2}$  |    |
| 14 | $\frac{14}{2}$ | $\frac{15}{5}$ | $\frac{15}{3}$ | $\frac{15}{5}$ | $\frac{16}{5}$ | $\frac{2}{3}$ | $\frac{15}{4}$ | $\frac{15}{3}$ | $\frac{16}{4}$  | $\frac{16}{3}$ | $\frac{16}{4}$  | $\frac{16}{3}$  | $\frac{17}{3}$ | $\frac{17}{2}$  | $\frac{17}{3}$  | $\frac{17}{2}$  | $\frac{17}{3}$  | $\frac{17}{5}$ | $\frac{17}{4}$  | $\frac{17}{3}$  |    |
| 15 | $\frac{15}{2}$ | $\frac{16}{5}$ | $\frac{16}{3}$ | $\frac{16}{5}$ | $\frac{17}{5}$ | $\frac{2}{3}$ | $\frac{16}{4}$ | $\frac{16}{3}$ | $\frac{17}{4}$  | $\frac{17}{3}$ | $\frac{17}{4}$  | $\frac{17}{3}$  | $\frac{18}{3}$ | $\frac{18}{2}$  | $\frac{18}{3}$  | $\frac{18}{2}$  | $\frac{18}{3}$  | $\frac{18}{5}$ | $\frac{18}{4}$  | $\frac{18}{3}$  |    |
| 16 | $\frac{16}{2}$ | $\frac{17}{5}$ | $\frac{17}{3}$ | $\frac{17}{5}$ | $\frac{18}{5}$ | $\frac{3}{2}$ | $\frac{17}{4}$ | $\frac{17}{3}$ | $\frac{18}{5}$  | $\frac{18}{3}$ | $\frac{18}{5}$  | $\frac{18}{3}$  | $\frac{19}{3}$ | $\frac{19}{2}$  | $\frac{19}{3}$  | $\frac{19}{2}$  | $\frac{19}{3}$  | $\frac{19}{5}$ | $\frac{19}{4}$  | $\frac{19}{3}$  |    |
| 17 | $\frac{17}{2}$ | $\frac{18}{5}$ | $\frac{18}{3}$ | $\frac{18}{5}$ | $\frac{19}{5}$ | $\frac{4}{3}$ | $\frac{18}{6}$ | $\frac{18}{5}$ | $\frac{19}{7}$  | $\frac{19}{5}$ | $\frac{19}{7}$  | $\frac{19}{5}$  | $\frac{20}{3}$ | $\frac{20}{2}$  | $\frac{20}{3}$  | $\frac{20}{2}$  | $\frac{20}{3}$  | $\frac{20}{5}$ | $\frac{20}{4}$  | $\frac{20}{3}$  |    |
| 18 | $\frac{18}{2}$ | $\frac{19}{5}$ | $\frac{19}{3}$ | $\frac{19}{5}$ | $\frac{20}{5}$ | $\frac{5}{3}$ | $\frac{19}{6}$ | $\frac{19}{5}$ | $\frac{21}{7}$  | $\frac{21}{5}$ | $\frac{21}{7}$  | $\frac{21}{5}$  | $\frac{22}{3}$ | $\frac{22}{2}$  | $\frac{22}{3}$  | $\frac{22}{2}$  | $\frac{22}{3}$  | $\frac{22}{5}$ | $\frac{22}{4}$  | $\frac{22}{3}$  |    |
| 19 | $\frac{19}{2}$ | $\frac{20}{5}$ | $\frac{20}{3}$ | $\frac{20}{5}$ | $\frac{21}{5}$ | $\frac{6}{3}$ | $\frac{20}{7}$ | $\frac{20}{5}$ | $\frac{21}{8}$  | $\frac{21}{6}$ | $\frac{21}{8}$  | $\frac{21}{6}$  | $\frac{22}{5}$ | $\frac{22}{4}$  | $\frac{22}{5}$  | $\frac{22}{4}$  | $\frac{22}{5}$  | $\frac{22}{7}$ | $\frac{22}{6}$  | $\frac{22}{5}$  |    |
| 20 | $\frac{20}{2}$ | $\frac{21}{5}$ | $\frac{21}{3}$ | $\frac{21}{5}$ | $\frac{22}{5}$ | $\frac{7}{3}$ | $\frac{21}{8}$ | $\frac{21}{6}$ | $\frac{22}{9}$  | $\frac{22}{7}$ | $\frac{22}{9}$  | $\frac{22}{7}$  | $\frac{23}{5}$ | $\frac{23}{4}$  | $\frac{23}{5}$  | $\frac{23}{4}$  | $\frac{23}{5}$  | $\frac{23}{7}$ | $\frac{23}{6}$  | $\frac{23}{5}$  |    |
| 21 | $\frac{21}{2}$ | $\frac{22}{5}$ | $\frac{22}{3}$ | $\frac{22}{5}$ | $\frac{23}{5}$ | $\frac{8}{3}$ | $\frac{22}{9}$ | $\frac{22}{7}$ | $\frac{23}{10}$ | $\frac{23}{8}$ | $\frac{23}{10}$ | $\frac{23}{8}$  | $\frac{24}{5}$ | $\frac{24}{4}$  | $\frac{24}{5}$  | $\frac{24}{4}$  | $\frac{24}{5}$  | $\frac{24}{7}$ | $\frac{24}{6}$  | $\frac{24}{5}$  |    |

The Table  
of Squares

Place this Table before D. and E.

| 21         | 22         | 23         | 24          | 25          | 26         | 27         | 28         | 29         | 30          | 31         | 32         | 33         | 34         | 35          | 36          | 37          | 38          | 39          | 40         |
|------------|------------|------------|-------------|-------------|------------|------------|------------|------------|-------------|------------|------------|------------|------------|-------------|-------------|-------------|-------------|-------------|------------|
| 1 3<br>5   | 4 6<br>9   | 4 4<br>5   | 5 5<br>6    | 3 5<br>7    | 5 5<br>10  | 3 5<br>16  | 2 5<br>16  | 1 5<br>3   | 1 5<br>3    | 1 5<br>2   | 1 5<br>8   | 1 5<br>4   | 1 5<br>10  | 1 5<br>8    | 1 6<br>6    | 1 6<br>14   | 1 6<br>8    | 1 6<br>4    | 1 1        |
| 2 6<br>5   | 2 6<br>3   | 6 6<br>6   | 7 7<br>7    | 7 6<br>6    | 7 7<br>14  | 7 7<br>9   | 7 7<br>2   | 7 7<br>3   | 7 7<br>4    | 7 7<br>8   | 8 8<br>6   | 8 8<br>4   | 8 8<br>3   | 8 8<br>2    | 8 8<br>2    | 8 8<br>4    | 8 8<br>2    | 8 8<br>1    | 2          |
| 3 8<br>6   | 8 8<br>6   | 8 8<br>2   | 8 8<br>3    | 8 8<br>2    | 9 9<br>8   | 9 9<br>6   | 9 9<br>3   | 9 9<br>2   | 9 9<br>3    | 9 9<br>8   | 10 10<br>8 | 10 10<br>6 | 10 10<br>4 | 10 10<br>3  | 10 10<br>2  | 10 10<br>1  | 10 10<br>1  | 10 10<br>1  | ?          |
| 4 9<br>5   | 9 9<br>3   | 9 9<br>2   | 9 9<br>4    | 10 10<br>10 | 10 10<br>5 | 10 10<br>5 | 10 10<br>5 | 10 10<br>5 | 11 11<br>11 | 11 11<br>8 | 11 11<br>2 | 11 11<br>2 | 11 11<br>3 | 11 11<br>4  | 12 12<br>12 | 12 12<br>3  | 12 12<br>2  | 12 12<br>2  | 12 12<br>2 |
| 5 10<br>4  | 10 10<br>2 | 10 10<br>4 | 11 11<br>11 | 11 11<br>6  | 11 11<br>4 | 11 11<br>2 | 11 11<br>2 | 11 11<br>2 | 12 12<br>12 | 12 12<br>2 | 12 12<br>2 | 12 12<br>1 | 12 12<br>1 | 13 13<br>13 | 13 13<br>5  | 13 13<br>2  | 13 13<br>2  | 13 13<br>1  | 14 14<br>1 |
| 6 11<br>4  | 11 11<br>2 | 11 11<br>4 | 12 12<br>12 | 12 12<br>2  | 12 12<br>3 | 12 12<br>3 | 12 12<br>3 | 12 12<br>3 | 13 13<br>13 | 13 13<br>2 | 13 13<br>2 | 13 13<br>1 | 13 13<br>1 | 14 14<br>14 | 14 14<br>2  | 14 14<br>2  | 14 14<br>1  | 15 15<br>1  | 15 15<br>2 |
| 7 12<br>4  | 12 12<br>2 | 12 12<br>4 | 13 13<br>13 | 13 13<br>4  | 13 13<br>3 | 13 13<br>3 | 13 13<br>3 | 13 13<br>3 | 14 14<br>14 | 14 14<br>4 | 14 14<br>4 | 14 14<br>3 | 14 14<br>3 | 15 15<br>15 | 15 15<br>7  | 15 15<br>7  | 15 15<br>6  | 16 16<br>16 | 16 16<br>3 |
| 8 13<br>4  | 13 13<br>4 | 13 13<br>4 | 13 13<br>4  | 13 13<br>4  | 13 13<br>4 | 13 13<br>4 | 13 13<br>4 | 13 13<br>4 | 14 14<br>14 | 14 14<br>4 | 14 14<br>4 | 14 14<br>3 | 14 14<br>3 | 15 15<br>15 | 15 15<br>7  | 15 15<br>7  | 15 15<br>6  | 16 16<br>16 | 16 16<br>3 |
| 9 14<br>4  | 14 14<br>4 | 14 14<br>4 | 14 14<br>4  | 14 14<br>4  | 14 14<br>4 | 14 14<br>4 | 14 14<br>4 | 14 14<br>4 | 15 15<br>15 | 15 15<br>4 | 15 15<br>4 | 15 15<br>3 | 15 15<br>3 | 16 16<br>16 | 16 16<br>4  | 16 16<br>4  | 17 17<br>17 | 17 17<br>5  | 17 17<br>5 |
| 10 15<br>4 | 15 15<br>4 | 15 15<br>4 | 15 15<br>4  | 15 15<br>4  | 15 15<br>4 | 15 15<br>4 | 15 15<br>4 | 15 15<br>4 | 16 16<br>16 | 16 16<br>4 | 16 16<br>4 | 16 16<br>3 | 16 16<br>3 | 17 17<br>17 | 17 17<br>2  | 17 17<br>2  | 18 18<br>18 | 18 18<br>4  | 18 18<br>4 |
| 11 16<br>4 | 16 16<br>4 | 16 16<br>4 | 16 16<br>4  | 16 16<br>4  | 16 16<br>4 | 16 16<br>4 | 16 16<br>4 | 16 16<br>4 | 17 17<br>17 | 17 17<br>4 | 17 17<br>4 | 17 17<br>3 | 17 17<br>3 | 18 18<br>18 | 18 18<br>3  | 18 18<br>3  | 19 19<br>19 | 19 19<br>4  | 19 19<br>4 |
| 12 17<br>4 | 17 17<br>4 | 17 17<br>4 | 17 17<br>4  | 17 17<br>4  | 17 17<br>4 | 17 17<br>4 | 17 17<br>4 | 17 17<br>4 | 18 18<br>18 | 18 18<br>4 | 18 18<br>4 | 18 18<br>3 | 18 18<br>3 | 19 19<br>19 | 19 19<br>6  | 19 19<br>6  | 20 20<br>20 | 20 20<br>5  | 20 20<br>5 |
| 13 18<br>4 | 18 18<br>4 | 18 18<br>4 | 18 18<br>4  | 18 18<br>4  | 18 18<br>4 | 18 18<br>4 | 18 18<br>4 | 18 18<br>4 | 19 19<br>19 | 19 19<br>4 | 19 19<br>4 | 19 19<br>3 | 19 19<br>3 | 20 20<br>19 | 20 20<br>19 | 20 20<br>19 | 21 21<br>21 | 21 21<br>4  | 21 21<br>4 |
| 14 19<br>4 | 19 19<br>4 | 19 19<br>4 | 19 19<br>4  | 19 19<br>4  | 19 19<br>4 | 19 19<br>4 | 19 19<br>4 | 19 19<br>4 | 20 20<br>19 | 20 20<br>4 | 20 20<br>4 | 20 20<br>3 | 20 20<br>3 | 21 21<br>21 | 21 21<br>4  | 21 21<br>4  | 22 22<br>22 | 22 22<br>5  | 22 22<br>5 |
| 15 20<br>4 | 20 20<br>4 | 20 20<br>4 | 20 20<br>4  | 20 20<br>4  | 20 20<br>4 | 20 20<br>4 | 20 20<br>4 | 20 20<br>4 | 21 21<br>21 | 21 21<br>4 | 21 21<br>4 | 21 21<br>3 | 21 21<br>3 | 22 22<br>21 | 22 22<br>4  | 22 22<br>4  | 23 23<br>23 | 23 23<br>8  | 23 23<br>8 |
| 16 21<br>4 | 21 21<br>4 | 21 21<br>4 | 21 21<br>4  | 21 21<br>4  | 21 21<br>4 | 21 21<br>4 | 21 21<br>4 | 21 21<br>4 | 22 22<br>21 | 22 22<br>4 | 22 22<br>4 | 22 22<br>3 | 22 22<br>3 | 23 23<br>22 | 23 23<br>8  | 23 23<br>8  | 24 24<br>24 | 24 24<br>8  | 24 24<br>8 |
| 17 22<br>4 | 22 22<br>4 | 22 22<br>4 | 22 22<br>4  | 22 22<br>4  | 22 22<br>4 | 22 22<br>4 | 22 22<br>4 | 22 22<br>4 | 23 23<br>22 | 23 23<br>4 | 23 23<br>4 | 23 23<br>3 | 23 23<br>3 | 24 24<br>22 | 24 24<br>8  | 24 24<br>8  | 25 25<br>25 | 25 25<br>1  | 25 25<br>1 |
| 18 23<br>4 | 23 23<br>4 | 23 23<br>4 | 23 23<br>4  | 23 23<br>4  | 23 23<br>4 | 23 23<br>4 | 23 23<br>4 | 23 23<br>4 | 24 24<br>23 | 24 24<br>5 | 24 24<br>5 | 24 24<br>4 | 24 24<br>4 | 25 25<br>23 | 25 25<br>8  | 25 25<br>8  | 26 26<br>26 | 26 26<br>3  | 26 26<br>3 |
| 19 24<br>4 | 24 24<br>4 | 24 24<br>4 | 24 24<br>4  | 24 24<br>4  | 24 24<br>4 | 24 24<br>4 | 24 24<br>4 | 24 24<br>4 | 25 25<br>24 | 25 25<br>7 | 25 25<br>7 | 25 25<br>6 | 25 25<br>6 | 26 26<br>24 | 26 26<br>7  | 26 26<br>7  | 27 27<br>27 | 27 27<br>4  | 27 27<br>4 |
| 20 25<br>4 | 25 25<br>4 | 25 25<br>4 | 25 25<br>4  | 25 25<br>4  | 25 25<br>4 | 25 25<br>4 | 25 25<br>4 | 25 25<br>4 | 26 26<br>25 | 26 26<br>7 | 26 26<br>7 | 26 26<br>6 | 26 26<br>6 | 27 27<br>25 | 27 27<br>7  | 27 27<br>7  | 28 28<br>28 | 28 28<br>7  | 28 28<br>7 |
| 21 26<br>4 | 26 26<br>4 | 26 26<br>4 | 26 26<br>4  | 26 26<br>4  | 26 26<br>4 | 26 26<br>4 | 26 26<br>4 | 26 26<br>4 | 27 27<br>26 | 27 27<br>7 | 27 27<br>7 | 27 27<br>6 | 27 27<br>6 | 28 28<br>26 | 28 28<br>7  | 28 28<br>7  | 29 29<br>29 | 29 29<br>7  | 29 29<br>7 |
| 22 27<br>4 | 27 27<br>4 | 27 27<br>4 | 27 27<br>4  | 27 27<br>4  | 27 27<br>4 | 27 27<br>4 | 27 27<br>4 | 27 27<br>4 | 28 28<br>27 | 28 28<br>7 | 28 28<br>7 | 28 28<br>6 | 28 28<br>6 | 29 29<br>27 | 29 29<br>7  | 29 29<br>7  | 30 30<br>30 | 30 30<br>7  | 30 30<br>7 |
| 23 28<br>4 | 28 28<br>4 | 28 28<br>4 | 28 28<br>4  | 28 28<br>4  | 28 28<br>4 | 28 28<br>4 | 28 28<br>4 | 28 28<br>4 | 29 29<br>28 | 29 29<br>7 | 29 29<br>7 | 29 29<br>6 | 29 29<br>6 | 30 30<br>28 | 30 30<br>7  | 30 30<br>7  | 31 31<br>31 | 31 31<br>7  | 31 31<br>7 |
| 24 29<br>4 | 29 29<br>4 | 29 29<br>4 | 29 29<br>4  | 29 29<br>4  | 29 29<br>4 | 29 29<br>4 | 29 29<br>4 | 29 29<br>4 | 30 30<br>29 | 30 30<br>7 | 30 30<br>7 | 30 30<br>6 | 30 30<br>6 | 31 31<br>29 | 31 31<br>7  | 31 31<br>7  | 32 32<br>32 | 32 32<br>7  | 32 32<br>7 |
| 25 30<br>4 | 30 30<br>4 | 30 30<br>4 | 30 30<br>4  | 30 30<br>4  | 30 30<br>4 | 30 30<br>4 | 30 30<br>4 | 30 30<br>4 | 31 31<br>30 | 31 31<br>7 | 31 31<br>7 | 31 31<br>6 | 31 31<br>6 | 32 32<br>30 | 32 32<br>7  | 32 32<br>7  | 33 33<br>33 | 33 33<br>7  | 33 33<br>7 |
| 26 31<br>4 | 31 31<br>4 | 31 31<br>4 | 31 31<br>4  | 31 31<br>4  | 31 31<br>4 | 31 31<br>4 | 31 31<br>4 | 31 31<br>4 | 32 32<br>31 | 32 32<br>7 | 32 32<br>7 | 32 32<br>6 | 32 32<br>6 | 33 33<br>31 | 33 33<br>7  | 33 33<br>7  | 34 34<br>34 | 34 34<br>7  | 34 34<br>7 |
| 27 32<br>4 | 32 32<br>4 | 32 32<br>4 | 32 32<br>4  | 32 32<br>4  | 32 32<br>4 | 32 32<br>4 | 32 32<br>4 | 32 32<br>4 | 33 33<br>32 | 33 33<br>7 | 33 33<br>7 | 33 33<br>6 | 33 33<br>6 | 34 34<br>32 | 34 34<br>7  | 34 34<br>7  | 35 35<br>35 | 35 35<br>7  | 35 35<br>7 |
| 28 33<br>4 | 33 33<br>4 | 33 33<br>4 | 33 33<br>4  | 33 33<br>4  | 33 33<br>4 | 33 33<br>4 | 33 33<br>4 | 33 33<br>4 | 34 34<br>33 | 34 34<br>7 | 34 34<br>7 | 34 34<br>6 | 34 34<br>6 | 35 35<br>33 | 35 35<br>7  | 35 35<br>7  | 36 36<br>36 | 36 36<br>7  | 36 36<br>7 |
| 29 34<br>4 | 34 34<br>4 | 34 34<br>4 | 34 34<br>4  | 34 34<br>4  | 34 34<br>4 | 34 34<br>4 | 34 34<br>4 | 34 34<br>4 | 35 35<br>34 | 35 35<br>7 | 35 35<br>7 | 35 35<br>6 | 35 35<br>6 | 36 36<br>34 | 36 36<br>7  | 36 36<br>7  | 37 37<br>37 | 37 37<br>7  | 37 37<br>7 |
| 30 35<br>4 | 35 35<br>4 | 35 35<br>4 | 35 35<br>4  | 35 35<br>4  | 35 35<br>4 | 35 35<br>4 | 35 35<br>4 | 35 35<br>4 | 36 36<br>35 | 36 36<br>7 | 36 36<br>7 | 36 36<br>6 | 36 36<br>6 | 37 37<br>35 | 37 37<br>7  | 37 37<br>7  | 38 38<br>38 | 38 38<br>7  | 38 38<br>7 |



## The Table of Timber measure, with the declaration and use of it.

15

## The x Chapter.

This Table (as ye see) is diuided into  
two Columnes or Rowes: the one ver-  
y short the other longer. In the head of  
the first, I haue put this word Foot: in the  
second row, Inches, and parts to signifie  
Feete, Inches, and parts of Inches. The  
summes in the marginne and left part of the  
first and second columnne, declare the quan-  
tity of the square of Timber or Stone from  
1. to 36. Inches square. Within the rowes  
you may finde the just length to a foote  
square, if ye enter into them in right order  
according to the square.

### **Example.**

Suppose the square of your Timber  
Were 7. Inches, and that yee desired to  
know what measure or length of the ruler  
would make a foote square : secke in the  
left margine, seuen Inches : and with him  
in that oyter toward the right hand, ye shall  
 finde 2. foote 11. Inches, and  $\frac{1}{2}$ . of an Inch.  
Note because the fraction  $\frac{1}{2}$  hath a prick by  
him, it betokeneth some small quantity  
lesse even  $\frac{1}{2}$ . of an inch. If it haue 2. prickes  
or points thus:  $\frac{1}{2}$ , it shoulde signifie some li-  
tle quantity more. Neither maketh it mat-  
ter whether ye obserue thys pricking or no,  
the quantitie is so little to be added or pul-  
led away.

Note what hath been spoken of timber,  
the same also is to bee understood of stone,  
likewise to be measured.

Thus is finished the measuring of Timber.

## **Now en sueth of Boord.**

HgW

# Tables, Boord, or Glasse.

How Tables, Boords, Glasse, or any such like,  
are measured, according to their length and breadth,  
only to the foote square.

## The xi. Chapter.

**T**his thing is performed by the helpe of a Table following, diuided in sixe small Tables, and as many Margins. The first and left Margin beginneth at  $\frac{1}{4}$ , which is one quarter of an Inch, and excedeth to sixe Inches, as yee may plainly perceiue if ye runne downe by that Margine. This hath his Table on the right side adioyning vnto him. The other taketh his beginning at sixe Inches,  $\frac{1}{4}$ . and endeth at twelue, having his proper Table also. The third from  $12\frac{1}{4}$  to 18. And so from  $18\frac{1}{4}$  to 24: from  $24\frac{1}{4}$  to 30. The last Margin is from  $30\frac{1}{4}$  to 36. and there endeth.

Of this that is said, you may gather that every Margin hath his Table on his right side. Also you must know that in the top, and beneath, I haue put (as in the Table of Timber measure) these words, Foote, Inch, and parts, to signifie, Feete, Inches, and parts of an Inch. Wherouer ye list to measure boord, Glasse, or any other such, with the breadth of it, enter this table, and seek that breadth in his proper margin; there ye shall finde in right order how many Feete, Inches, or parts of an Inch, belong to a Foote square. So often as the measure is in your stuffe, iust as many Feete haue ye in that Boord, or such like. If the breadth exceed this Table, then diuide the breadth in parts, and worke as is and shall be declared. So the ingenious appliech this Table for all manner breadths, most exactly.

Example.

|   | Fo | YH | Fo | YH | YH Par | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 48 | 0  | 1  | 11 | 1      | 3      | 7      | 15     | 3      |
| 4 |    | 4  | 1  | 11 | 2      | 4      | 7      | 16     | 4      |
| 1 | 24 | 6  | 1  | 10 | 1      | 2      | 4      | 7      | 10     |
| 2 |    | 2  | 1  | 10 | 2      | 11     | 2      | 5      | 2      |
| 3 | 16 | 6  | 2  | 1  | 2      | 2      | 7      | 10     | 3      |
| 4 |    | 4  | 1  | 2  | 4      | 11     | 4      | 4      | 3      |
| I | 12 | 7  | 11 | 8  | 4      | 13     | 11     | 19     | 7      |
|   |    |    |    |    |        | 16     | 4      | 25     | 5      |
|   |    |    |    |    |        |        | 7      | 25     | 4      |
| 1 | 9  | 7  | 1  | 7  | 1      | 7      | 1      | 25     | 1      |
| 4 |    | 5  | 7  | 4  | 1      | 8      | 2      | 4      | 5      |
| 1 | 8  | 1  | 2  | 1  | 7      | 13     | 2      | 25     | 1      |
| 2 | 2  | 1  | 2  | 1  | 13     | 2      | 13     | 2      | 4      |
| 1 | 6  | 10 | 2  | 7  | 4      | 6      | 7      | 25     | 5      |
| 2 | 6  |    | 8  | 1  | 6      | 14     | 10     | 25     | 1      |
|   |    |    |    |    |        | 2      | 7      | 5      | 2      |
| 2 | 4  | 9  | 8  | 4  | 1      | 5      | 3      | 20     | 4      |
| 1 | 2  | 4  | 9  | 3  | 8      | 1      | 4      | 15     | 7      |
| 2 | 2  | 4  | 9  | 3  | 8      | 1      | 4      | 15     | 7      |
| 2 | 3  | 4  | 4  | 8  | 3      | 1      | 4      | 15     | 7      |
| 3 | 4  |    | 9  | 1  | 4      | 15     | 9      | 21     | 6      |
| 3 | 4  | 3  | 8  | 1  | 9      | 1      | 4      | 21     | 6      |
| 3 | 4  | 3  | 8  | 1  | 9      | 1      | 4      | 21     | 6      |
| 3 | 2  | 3  | 5  | 8  | 2      | 1      | 2      | 21     | 5      |
| 3 | 3  | 4  | 2  | 5  | 9      | 2      | 1      | 21     | 5      |
| 4 | 3  |    | 10 | 1  | 2      | 5      | 16     | 9      | 22     |
|   |    |    |    |    |        |        |        |        | 6      |
|   |    |    |    |    |        |        |        | 28     | 5      |
|   |    |    |    |    |        |        |        | 3      | 4      |
| 4 | 12 | 9  | 10 | 4  | 1      | 2      | 21     | 16     | 8      |
| 4 |    | 8  | 10 | 4  | 1      | 2      | 21     | 16     | 8      |
| 4 | 1  | 2  | 8  | 10 | 1      | 3      | 16     | 1      | 22     |
| 4 | 3  | 2  | 6  | 10 | 1      | 3      | 16     | 1      | 22     |
| 5 | 2  | 4  | 11 | 1  | 1      | 1      | 17     | 3      | 23     |
| 5 | 4  | 2  | 3  | 11 | 1      | 1      | 17     | 3      | 23     |
| 5 | 2  | 2  | 2  | 11 | 1      | 1      | 17     | 3      | 23     |
| 5 | 3  | 2  | 1  | 11 | 1      | 2      | 17     | 3      | 23     |
| 6 | 2  |    | 12 | 1  | 1      | 18     | 8      | 24     | 6      |
|   |    |    |    |    |        |        |        | 30     | 4      |
|   |    |    |    |    |        |        |        | 36     | 4      |
|   |    |    |    |    |        |        |        |        | YH     |

# The Art of measuring

## Ensample.

Suppose I haue a pane of Glasse, or a Boord, whose breadth were 22. inches,  $\frac{1}{2}$ , the length 15. foote. In the fourth margine, I finde this breadth, 22. and  $\frac{1}{2}$ . And even with it in the table rightward, I see 6. inches,  $\frac{1}{2}$ . So much of my Ruler wanting some small quantity, maketh a foote.

Now because in the length of my boord(which is 15. foote) that measure is found 29. times, and  $\frac{1}{2}$ . parts: I conclude 29. foote there to be, and two third parts of a foote & square, according to the length and breadth I said ( wanting some small quantity) because of the point ioyned to this fraction  $\frac{1}{2}$  which is put to diminish the fraction some little thing, as is declared plainly in the other Tables before put forth.

**H**E that desirereth to measure chamber floores, pavements, Ho<sup>r</sup> such like, let him only multiply the breadth with the length, so the product sheweth the Content.

## Ensample.

If there were a pavement 100. foot long, and in breadth 50. I must needs conclude (by multiplication of the length in the breadth there to be contained 5000. foote.

Or thus without Arithmetike, when the breadth exceedeth the Table.

**D**uide the breadth in parts (as is opened in the Declaration of the table of account) and worke as I haue before instructed. So for pavements all manner waies it serueth your turne. Of this matter to put forth tables, were superfluous cediousnesse and folly. The ingenious with these few will be satisfied.

The

## The Carpenters Ruler.

The face of the Carpenters Ruler, figured with the true measures, and other things necessary.

### The xiij. Chapter.

Because the effect of this ruler is above declared by tables, an instrument also wel knowne and common among good Artificers, I will not spend many words in opening it. Behold þ figures & leavue by the how ye ought to make, and commonly to decke your Ruler, both with timber and boord measure.

#### Ensample.

Admit the Ruler to be a. b. 18 c. d. well plained 12. Inches long, a quarter of an Inch thick, & 2. Inches in breadth. 17 Truly it were more cominodious, if it had two foote in length. This ruler here imagined, but a foote long is diuided first in 12. even parts called inches : then every inch in halfe, or two equall portions : each halfe in two quarters : every quarter in four 14 of 2. parts at the least : as in this ensample. Then are the figures placed from 1. to 12. 13 manifesting the inches. Thus your ruler is ready to receive the measures which are marked or figured on your Ruler thus. Above first the timber measure as followmeth.

### Timber measure

|                      |                       |  |    |
|----------------------|-----------------------|--|----|
| 144                  | 32                    |  |    |
| 36                   | 6                     |  |    |
| 2                    |                       |  |    |
| 16                   | 4                     |  |    |
| 3                    |                       |  |    |
| 9                    | 3                     |  | 36 |
| 4                    |                       |  | 33 |
| 5.9. $\frac{1}{2}$   | : 4. $\frac{4}{5}$    |  | 30 |
| 5                    |                       |  | 27 |
| 4                    | 2                     |  | 42 |
| 6                    |                       |  | 22 |
| 2. 11. $\frac{2}{3}$ | : 1. 8. $\frac{4}{5}$ |  | 20 |
| 2. 7                 | 1. 5                  |  | 19 |
| 8                    |                       |  | 18 |
| 2. 4                 | 1. 4                  |  | 17 |
| 9                    |                       |  | 16 |
| 17                   | 2                     |  | 15 |
| 10                   |                       |  | 14 |
| 14. 2                | 1. 1                  |  | 13 |
| 11                   |                       |  |    |
| 14                   |                       |  |    |
| 12                   |                       |  |    |

### Boord measure.

## The Carpenters Ruler.

**S**hall resoxt to your table of Timber measure, and seeke how many feete belong to one Inch square: there yee shall finde 144. This number note, write, or rather graue, where this figure 1. representing one Inch, is figured as yee may see in the middest betweene the line c. f. and the line g. h. This done, resoxt to your table agayne, and beholde how many feete and parts two Inches square requireth. So shall yee finde 36. foote, which is placed in the next roome lefftward, vnder the Character 2. signifying two Inches. Thus the rest, feete, Inches, and parts, found in your table, vntill you come to the 12. Inch, where ye shall perceiue twelve Inches onely to bee set in his proper roome, &c. Then seeke further in your table what belongeth to 13. Inches. Loe tenne Inches and  $\frac{1}{2}$ . This must be numbered in the line c.d. from c. which line betokeneth the thicknesse of the Ruler. Make ther a little strike vpon that grossenesse, euen or right against the measure 10. What neede many words? Thus doe vntill you come to 36. Inches, and that is noted (as the table of timber measure sheweth) right with one Inch and  $\frac{1}{2}$ , from c. No otherwise is performede of boord measure, as ye may behold set forth by the helpe of his proper table in the Square roomes beneath the line c.f.  
and also the other thicknesse  
of line b. a.

the quadrant Geometricall.

## The backside of the ruler.

### Lyre of Scans.



### The xij. Chapter.

This other figure i. k. l. m. The making is the backside of your ruler, having in the middest of call quadrant. Geometricall quadrant n. o. p. q. whose making in few words is thus exprested. The line or breadth of your ruler n.o.the line o. p.p.q.q.n. ought to be of one equall iust length, cutting each other squirewise. And from the center n. unto p. is drawne another line, three principal which is called the line of lines. Note these beight. So is o. n. the line of leuell, q. n. the line of heights vnyght. This knowne, I open my compasse, one foote remaing. In the center n. the other extended in the line of leuell al- most to o. making a circumference to q. n. which is a portion of a circle named a quadrant, and ought to bee diuided into 90. equall parts, as ye may be- hold, every of them called a de- gree. Ye may diuide the lines o.p.p.q. named the Scale, each The diuided in 12. as here, or in 60. yea in sides o.p. and 100. equall portions is more p. q. are called meete for the use of shadowes, the Scale. heights, lengths, &c. Note that the line or halfe Scale o.p. is called the contrary shadow p. p. right shadow. Remember that vpon the thicknesse m. k. ye ought to haue two fine e- quall square sights well boord, represented here by r. s. made of wood, or rather metall to bee fastned there when time requi- reth.

The common vse of the Carpenters Ruler,  
touching the Face afore put foorth.

The xiiiij. Chapter.

The eight  
Chapters shew  
eth how the  
true square is  
found.



Oppose a piece of timber to bee moaten, whose true square is 7. Inches, this square appointed you to the figure of 7. in the line g. h. under whom rightward in the place assigned to Timber measure, is written 2. foote, 11. inches,  $\frac{2}{7}$ . As often as that measure is found in the length of your timber, so many foote of timber is in that piece.

Another Ensample.

I **H**agine your Square to be 22. Inches: seeke in the line l. o. c. Note then how much of your Ruler is left from that to the end of your Rule c. and so much belongeth to a Foote. Therefore lay out the measure upon your timber, and reckon how many times ye may finde it, from the one to the other of your Logge: soz so many foote of timber is there. Even thus of boord. Seeke the bredth upon your Ruler, in the roome or place of boord measure, and immediately before your eyes there remaineth what is to be laid out to make a just foote of boord.

The vse of the principall lines in the Geo-  
metricall Quadrant on the backside of the Ruler,  
and first of the leuell line.

The xv. Chapter.

I **H**ebooueth you to looke thowz your sightes q. n. placed in the thicknesse or line. k. m. a fine thred and plummet falling at liberty out of the Center n. If this plummet and thred chance precisely on the line of leuell (which is n.o.whatsoeuer ye see thowz the sight, is leuell with your eye; if otherwise

wise the thing that yee looke unto is not leuell, either more or lesse then the height or leuell of your eye: Note, if the plummet fall to you-ward: lesse, if contrary.

**H**ow by the line of Leuell to foresee, whether the water of any Spring or head is possible to be brought to a place appoynted, and also to judge the wholesomnesse of it.

*The xvi. Chapter.*

**S**hall goe to the head of Spryng, and set your Ruler to your eye (being in height equall with the water) so that the fine cord and plummet fall precisely in the line of levell. Now, if through the lights yee may see aboue the place, know and judge the water possible to be brought: if your sight fall under, impossible. It commeth commonly to passe, when the place to which yee would haue water conveyed, is of any great diuance from the head, then Hilles, Valleys, and such like impediments, let the line visuall to haue his free course: wherefore this remedy is prouided: At the head of the Spryng, yee shall looke thowzow the lights (as before) and note a marke in the next Hill toward the place: then goe to the marke: in like manner obserue another in some hill: so forth, untill by any of them yee may perceiue the place desired. If then your sight running thowzow the pinnes of your Ruler (the chyd euer falling on the Line n. o.) exceede that place, the conveying of your water is possible. Otherwise not.

Now by the way briesly yee shall be instructed, how yee may know the wholesomnesse of water.

**H**ow good water is knowne.

**T**ake a cleane pot, and put water in it: so set it on the fire: after a little boylung, powze it out: if then no filth remaine

## The vse of the, &c.

maine in the bottome of the pot, it may be iudged the wholesomer. Or thus. Let fall drops vpon metall, or rather on Glasse (any of them being polished) and suffer that to drie by it selfe: if after there remayne no spot or signe, it is a good token. Moreo-  
uer if your water be sweete, pure, cleare, light, or of little-  
weight, it followeth, the water to bee wholesome for the vse of  
man.

## Of the Line of height.

**V**hensoever the Thred and Plummet doe chance to st-  
ly on the Height, which is n. p. the Altitude or  
height that ye see, is even with the distance from the middle  
of your Foote, to the nether part directly vnder the toppe, e-  
quall with your standing, adding the height of your Eye  
downeward. Know that ye must euer stand upright with  
boodie and Necke, your Feete iust together, the one Eye clo-  
sed, &c.

## The line of vpright Altitudes.

**I**udge also any thing plumbe vpright, when the thicknesse of  
your Ruler i. l. is closely thereon, the plummet then at li-  
berty falling on q. n. named the Line of Heights vpright. Now  
followeth the vse of the Scale,

## To search out Heights by the Scale, with the aid of two places.

### *The xvij. Chapter.*

**I**n the Thred and Plummet fall in the one, on the  
12. pointes; in the other Station, on the 6. of the  
right shadow: double the distance betweene the  
two places, the summitis appeareth from that part of  
the thing measured, which is equall in Height with your  
eye.

eye. Or the one in the 12. the other in 8. of right shadow: then triple the distance. The one in 12. the other in 6. of right Quadruplicate, the space. The one in the 12. the other in 6. of the contrarie shadow: then the space betweene both the Creations is eqnall with that yee measure, euer understanding from your eye upward. Euen that same commeth to passe, if in the one the Thred bee found vpon the 6. of the contrarie, in the other on the 4. of the same, or the 4. and 3. of the contrarie. In all these the spaces are equall with the Altitudes. So then, in measuring the distance betweene the two places, yee haue the height from your eye upward, putting to it the length from your sight downward, the whole altitude appeareth, the Base being equall with your standing.

I would not haue you ignorant here, how to know lengths which be in height not easie to come unto. For ( as before ) get the height of the toppe, the Altitude of the Base or longest part of your length. Subduct the lesse height out of the moxe, of force your desired length remaineth. Or thus: Let the plumm-  
met and thred fall in the 12. Marke your place: goe in to-  
ward the thing (the thred as it was) vntill yee see the Base of  
that length: the distance betweene the two standings, is undoubt-  
edly the Length. How lengths  
in height are  
knowne.

### How with the Scale direct or vp-right heights by their shadowes are declared.

#### *The xix. Chapter.*

**T**urne your left side vnto the Sunne, suffering his Beames to pearce both your sightes q. r. placed ( above is sayd ) in the thicknesse or line k. m. The Thred or plummert then hanging at liberty, out of the Center n. sheweth as well the Degrees  
F 2 of

## THE VIE OF THE

of height to be counted from o. as the parts of the Scale cut. If your thred be found in the 12. part or line of leuell, Shadewes of all things being perpendicular elevated, are equal with their bodies. If the plummet with the thred be perceiued, cutting the parts next to the lights, which I name poynts of the right shadow, then every thing direct is more then his shadow, by that proportion which 12. exceedeth the parts, where the thred was found. If it fall in l. that is the first part of the right shadow, take the shadow twelue times to make the height. In two, that is the second part, sixe times, in the third, fourre times : in the fourth, three times : in the fift, twice : and  $\frac{1}{3}$ . of the shadow, in the sixth, twice, in the seuenth once, and  $\frac{1}{4}$ . in the eighth once, and  $\frac{1}{2}$ : in the ninth once, and  $\frac{1}{3}$ : in the tenth once, and  $\frac{1}{8}$ : in the eleuenth ye shall take the shadow once, and  $\frac{1}{12}$ . part of it.

Right shadow. If the Arte of numbyng were had, I would will you to multiply the length of the shadow by 12. and the product diuide by the parts, in the which you found the thred.

Contrary shadew. But if it bee in the parts of the contrary shadow, augment the length of the shadow with the parts declared by the plummet: and the increase diuide them by 12. so commeth the altitude also.

Thus the composition and whole appliance of the Carpenters Ruler is shewed: therefore somewhat shall be now said of the Squire.

I am not ignorant that the common use of him, is better knowne then I can with many words expresse, wherefore I leauie to write in that behalfe. Notwithstanding I will declare how Heights and Lengths are taken, &c. matters rare and knowne of few Artificers.

Also by tables to get a true knowledge of the day-hour, and that divers waies, with the helpe of the Squire, as is opened in my generall Prognostication, augmented in the yeere of our Lord 1556.

What

What length the sides of thy Squire ought  
to bee, and the diuision of him.

*The xx. Chapter.*

I Meede not to put forth  
the exact making of this  
Instrument so wel knowne:  
Loe therefore the figure:  
One side supposed two foote  
from the inward Angle:  
and the other a iust foote  
from the same. The longer  
a.b. inwardly diuided from  
the Angle a. unto b. into  
24. equall princiiall parts,  
and every of them into a  
lesse (if ye list) each contai-  
ning 10. minutes. Also the  
side c.d. in the outward con-  
trary, plaine from the top  
c. unto d. is diuided into 12  
euene portions: and againe  
(if ye require exactnesse) e-  
very of them into 6. each of  
a value 10. Minutes: Behold a line and plummet falling from  
e. to f. a Parallelle to c. d. and a. b. Thus this squire is well  
framed for the use of divers Tables put forth in my generall  
Prognostication, and also for the finding of Altitudes and Lon-  
gitudes, which here I purpose now briefly to open.



How by the Squire heights are knowne.

A ltitudes or heights are found, the line or plummet cen-  
tered in the sixt poynt, cutting h. the middle of a. g. The  
mooueable

## The vies of the

mooueable sightes placed in a. g. o) a parallell from that line  
not unlike, as is opened of the line of height, in the backe of my  
Ruler,

### How Lengths in plaine Ground are searched by the Carpenters, or Masons Squire.

*The xxi. Chapter.*

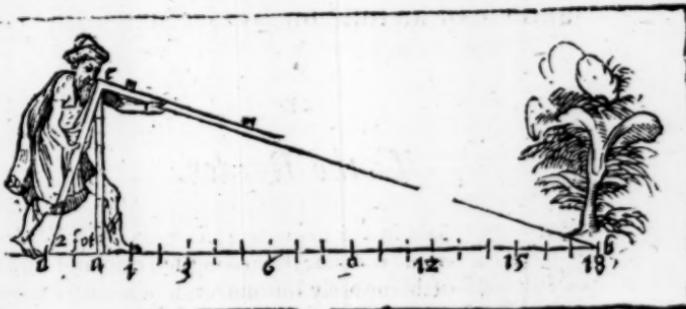
**H**ake a staffe diuided into certaine portions as  
pee list, in a 100. or a 1000. parts. At the be-  
ginnig of your length, vpon the very top  
directly standing, set the inward Angle of  
the Squire : lift vp, or put downe this in-  
strument, vntill you see the furthest part of  
your Longitude, I meane, vntill your sight running from that  
Angle, to the end of your Squire, come unto the furthest parte  
of that length. The Squire so remaining, and the Staffe not  
remooued from his height; marke where the other end of the  
Squire next unto you noted vpon the ground. See what pro-  
portion the Staffe then beareth to the part of the ground,  
which the nearest end of the Squire pointed unto from the  
Staffe : the same shall the Length haue to the quanticie of the  
same Staffe.

### Example.

The cause is  
taken out of  
Enclid 33. pro.  
x. booke and  
the 4. pro. 6.  
booke.

**T**he Staffe a. c. in this figure is imagined 6. Foote, and  
the space a. d. 2. Foote. Considering now that 6. the  
length of the Staffe containeth 2. thrice, therefore the Lan-  
guishesse desired, a. b. of foote must containe thre times the  
Staffe (which Staffe is 6. Foote) that maketh 18. Foote. As  
this is prooued true by a small ground in the figure follow-  
ing: so the arte faileth not in a greater space, whiche the good  
*Speculator*,

Speculator and diligent practicer by any way cannot denie. Yet experience willer me this to confesse, that the Squire is not conuenient for any long distance, but the Instrument Geometrical (whose making and use ye may perceiue in the Treasise following) unlesse ye ascend some Tree or Turret for your ayre, which length knowne, shall stand in stead of your Staffe.



### A Note.

**I**T behooueth you to haue a fine cord, made fast in the vpper part of your Staffe.c. which shall bee tied even with the inward edge of the Squire, and so drawne to the ground, where the neare end of the Squire from the Staffe pointed, as yee see d. c. the other end then truly directing to the furthest di- stance.

Know that the ground must be very plaine and leuell, o- therwise error ensueth.

Thus the use of the Squire is here somewhat declared, but more in my generall Prognostication, yea most plentifully hereafter (God sparing life) in a Booke titled, The rare use of the Squire in practices Mathematicall. In the which Booke, profitable pleasant experiences shall bee plainly opened (only of me practised) as well of Perspectiue, as of the Mathemati- cals in generall.

A



A little Treatise, declaring the making  
and vse of an Instrument Geometricall, so  
farre as it furthereth the Landmeater or Car-  
penter, named the profitable  
Staffe.

*To the Reader.*

**I**Said in the beginning, that no little Booke would containe the making and manifold fruits of this princely Instrument, if it were set forth as it ought to be in his perfection. Certes the truthe euen here maketh me confesse the same : yea, that there is no Instrument so generall and profitably pleasant: Notwithstanding know (gentle Reader) that the occasion of his chiefe vse and profit is not here ministred : neither, to say the truth, doth it appertaine to, or agree with the capacity of such Artificers. Therefore I shall leue to intreate of his ample large vse and best making, and will set him forth in few words : yea sufficiently for the Land-meaters capacity or Carpenters purpose, that at the least they may receiue some kinde of fruite with the Geometrre. And in time to come (by other meanes) as I see cause, I will largely declare, and there decke him with his proper beauties. Here now followeth the making, and so briefly, how he is applied for the profit of the aforenamed Artificers.

The



TABVLA C

| 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 |   |
|----|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| 1  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 |   |
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| 3  | 2 | 1 | 3 | 3 | 4 | 2 | 5 | 1 | 6  | 3  | 7  | 2  | 8  | 1  | 9  | 2  | 1  | 2  | 3  | 3  | 4  | 1 |
| 4  | 4 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 1  | 2  | 1  | 3  | 4  | 1  | 5  | 2  | 6  | 7  | 8  | 9  | 1  | 2 |
| 5  | 6 | 1 | 7 | 2 | 8 | 3 | 1 | 1 | 2  | 2  | 3  | 3  | 5  | 1  | 4  | 1  | 2  | 2  | 2  | 3  | 3  | 2 |
| 6  | 9 | 1 | 2 | 2 | 3 | 2 | 5 | 6 | 2  | 8  | 1  | 2  | 1  | 2  | 2  | 4  | 5  | 2  | 7  | 8  | 2  | 3 |
| 7  | 2 | 1 | 4 | 1 | 5 | 3 | 7 | 2 | 9  | 1  | 1  | 2  | 3  | 4  | 2  | 6  | 7  | 3  | 1  | 2  | 3  | 3 |
| 8  | 6 | 1 | 8 | 1 | 2 | 2 | 4 | 6 | 8  | 2  | 2  | 3  | 3  | 4  | 3  | 5  | 3  | 3  | 4  | 1  | 2  | 4 |
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| 11 | 3 | 1 | 3 | 3 | 3 | 3 | 3 | 1 | 2  | 1  | 4  | 1  | 3  | 3  | 2  | 2  | 1  | 5  | 7  | 3  | 1  | 2 |
| 12 | 6 | 3 | 3 | 2 | 1 | 5 | 3 | 2 | 1  | 5  | 3  | 2  | 1  | 5  | 4  | 7  | 3  | 5  | 6  | 1  | 2  | 4 |
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| 15 | 6 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2  | 2  | 2  | 2  | 2  | 2  | 3  | 1  | 5  | 8  | 3  | 2  | 2  | 1 |
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| 22 | 1 | 2 | 2 | 1 | 4 | 2 | 1 | 2 | 2  | 1  | 4  | 2  | 1  | 4  | 2  | 1  | 4  | 2  | 1  | 3  | 4  | 2 |

Place this Table after the White page in C.

# COMPUTATION

| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
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| 26 | 2  | 2  | 2  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 24 |
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| 28 | 2  | 2  | 2  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 3  | 26 |
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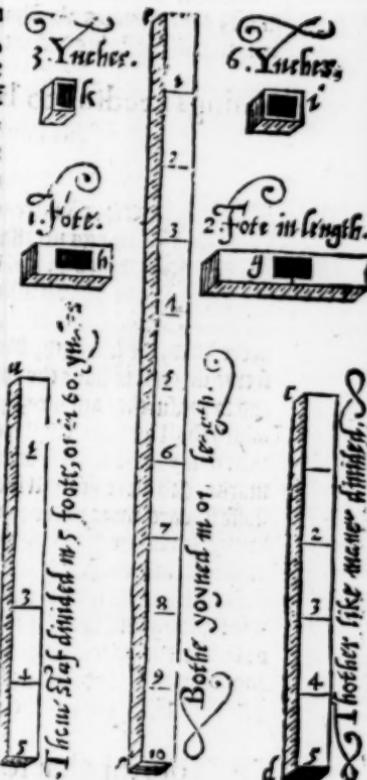
1900-1901

The making of this profitable  
Rodde or Staffe.

**Y**e shall prepare two small, straight, stiffe, round, or rather square Rods, of metall or of wood, well plained, of like bignesse and length. Although it make no matter of what length, yet to auoyde the errors, which little instruments, and shoxt staves bring, and also to bear with the rude unwanton handling of such Artificers: let your Rods be each ffe, or at the least three foote, and every foote diuided in 12. even parts or Inches, as yee see a. b. and c. d. These Rods must be forged with a vice in the end of them to ioyne readily ten or sixe foote in length, (when time requireth) as the figure e. f. sheweth. Also yee must get (by the helpe of some Craftsman) foure other like Rods, the longer g. 2. Foote: the next h. 1. foote: the other i. 6. Inches, then k. 3. Inches, the last and shortest l. 1. Inch, and m. Each of these must haue in their middest a hole, that the long staffe of ten foote may bee put thoroþ them, and they moþued on him at pleasure by and downe, alwaies cutting the longer staffe e. f. Quitewise, and made to carry on any diuision, as occasion shall be giuen: which all are easily to be perceaved

G

by



## The vle of the

by the figure following, although my rude declaration hath not expressed my meaning.

Here note in the stead of your shor staves, ye may haue one crosse staffe two foote long, with currant sightes, so artificially made, that alwaies the shor staffe shall run squire vpon the longer, and the sightes distant, as ye list to place them.

## Things needfull to be knowne before the vse of this Instrument is opened.

### *The ij. Chapter.*

**B**EFORE I intreate of this vle, it behooueth to know things necessary, and first, which of the fve little staves g. h. i. k. l. mentioned in the making, is to be put vpon your long staffe e. f. according to the distance of the marke. Note if your marke bee neere hand, be it length, breadth, or height, the longer g. both seeme meetest to haue the roome, if more of length, the other h. and so the further distance, the shorster the staffe requireth to be, which shall occupy that place. Oft practice sheweth this better then many words. Also note, if chance be to goe in toward your marke, (as after ye shall see how) you must remooue the shor staffe inward more neere to the end of the longer e. If pee bee compelled to goe from it, then put it from e. toward the end f. Also remember when ye are appoynted to measure any breadth or length (as shall be declared) it behooueth you to stand right with, and against that breadth: yea and the longer the breadth, or larger the widenesse or length is, the better the thing will come to passe. And for heighes it is necessary (if yee regard all precisenesse) to haue the height stand direcly vp.

Note this that followeth to be generall  
in all workings.

**Y**OU must stand right vp with your Bodie and necke, your feete iust together, your hands not much mouing, the one eyne

eye closed, and ever marke your ſtanding right with the midſt of your ſteete. Be not ignorant here, that I call the extremes of the little ſtaues, the very ends where the ſight ever runneth. And no diſference betweene the Altitude and height, betweene the Longitude and length: the Latitude and breadth. The ſhorter ſtaues I name by the letter figured ouer them. Your eye muſt ever be placed in the end of the longer ſtaffe c. and with the other eye ye ought to winke.

What these  
words meane,  
Longitude,  
Latitude,  
Altitude.

These trifles and ſuch like omitted, letteth the truthe to come to paſſe, and make men to ſuspect the Ground, which is moſt certaine.

### How heights ſtanding directly vp, are measured by the Inſtrument.

#### *The ij. Chapter.*

**P**ut the ſtaffe g. vpon the longer c. f. any mooue him his iuft length from the beginning of the longer c. turne the ends of g. toward you, and according to that height placing your eye (as is ſaid) ever at the beginning of the longer c. with the other eye winke. Then goe backe vntill you may plainly perceiue the very upper part of that Altitude, and alſo the lower end by the extremes of your ſhorter ſtaffe g. Now the ſpace of the middle of your ſoote to the base of the height, is equall with the Altitude.

#### Or thus.

When you ſhall ſee any Altitude, whose measure ye require, imagine by coniecture how oftentimes that height is found in the ſpace from it vntill your ſtanding. Then mooue your ſhorter ſtaffe (choſen as aboue moſt conuenient) euен as often his owne length from the beginning of the longer c.

## THE VIE OF THE

where your eye is euer placed. This done, turne the ends of your little staffe, your eye being in c, according to the height: looke whether ye may see by the extremes of your shoxter the very top, and also the lowest part of the height. If not, mooue the shoxter a lenghb further toward f, or neere to c, as yee see cause, and as your conjecture failed. ¶ let your little staffe remaine, as by conjecture he was put, and goe toward o from that height, vntill the Altitude agree iustly with the extremes of your shoxter staffe. Then marke that place with the middest of your foote.

Now ye may conclude, that the height is as often contained in the distance, which is betweene the marke and it, as the lenghb of that little staffe is found remooued from the end of the longer, &c.

### Example.

How the iust  
height is  
knowne.

If the shoxter staffe bee ten times his owne length from c, af-  
firme the height contained in that distance ten times onely.

The Altitude is thus gotten. Mooue your shoxter staffe from his late being a length either toward o from c, as ye list to goe in o backe. Then goe fro o neere unto it (as before) vntill the very summity, and also the lowest part of the height agree with the extremes of your shoxter staffe. The space then betweene your marked place and this latter, declareth the iust height. Oftentimes through impediments, yee shall not haue roome to goe so farre backe o forward, as the height commeth vno.

A remedy pro-  
vided for want  
of ground.

This remedy is provided: Mooue the little staffe halfe his length, and so leake two stations (as before) vntill the extreme of the shoxter staffe be found iustly to answere either end of the height. Then the space betweene the two standings must bee doubled, to haue the iust height: or if ye list, ye may mooue the shoxter, according to the fourth part of his length, o to any por-  
tion, as to the fifth, sixt, twentie, &c. then shall ye haue that part of the height betweene the two stations.

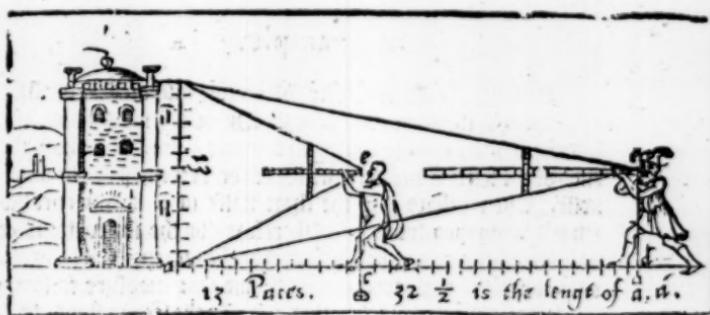
Yet know this (which experience by diligent practice will  
shew)

shew) the bigger parts yee take, the lesse errore yee commit. A little errore often multiplied, encreaseth to a great.

Now that all the aforespoken may the better be perceived, behold the example ensuing, as ye may see by figure declared, in this may be gathered of Euclide in his perspective. 21. Theo.

the which the heighth is imagined a. b. the first station c. the shorther staffe g. is moued from c. lenth his length. I am forced to conclude, that the Base of the heighth a. b. is from my standing c. even his preesse length. So then, if ye measure that distance of a. c. being 13. paces, ye haue the true heighth of a. b. as many. In the other standing place d. the shorther staffe is found from c. twice his length and a halfe, wherefore I must assieme the heighth a. b. to bee contained or found in the distance a. d. twice and a halfe: which length a. d. is apparant 32. paces. All this that is spoken of the heighth, may well be understood of Latitudes or widenesses, and lengths following.

In Altitudes this rule is not perfect, except the eye be leuell with the middle of the Altitude.



How the breadth or widenesse of things  
are found, and by them, Length or any  
distance at pleasure.

*The iiiij. Chapter.*

**W**hatsoeuer I haue instructed afore of heights, the same understand here of widenesse, lengths, &c. For none otherwise are Latitudes or widenesse searched by this Instrument, then before is declared of heights, onely this excepted, that the short staffe must lie contrary, the ends according to the breadth, seeing by the extremes of the short staffe, the very uttermost parts or ends of the Latitude, noting your stations right with the middest of your foote: And so performe all as tofore. And as I said, thereof the parts of the height found betweene your standings, even the same thing is well vsed here, for all manner parts of the breadth.

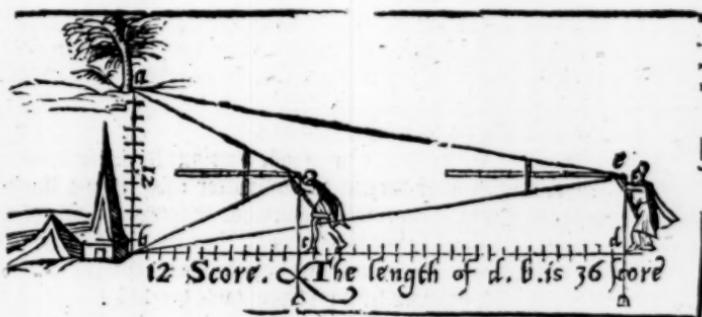
*Example.*

**T**he breadth in this figure following supposed a. b. Also the first station c. the next d. My desire is to know the widenesse a. b. and the length or distance d. b. Marke how the ends of the lesser staves are turned to the extremes of the widenesse. Then behold how the short staffe in c. is but once his length remooued from c. Wherefore (by the instructions of heights afore) ye may boldly say, that the widenesse a. b. is but once contained betweene d. and b. and that measure is found 12. scope, as much as is the other a. b. In the second standing d. the little staffe is remooued three times his length from c. For that cause I conclude (and truly) from b. to that station three times the breadth, which breadth is 12. scope. So by the widenesse I haue found the length of b. d. 36. scope, my desire. Thus are Latitudes found, and by them Lengths, &c.

Behold

## Behold the Figure.

Ye must alway stand directly against the middle of the Breadth.



Whensoeuer any distance is put, whose certaine length yee require: measure (by the art expressed) either the heighe of any thing there found, or the breadth, and see how often-times that widenesse or length is contained vnto your standing: which knowne, the length cannot bee hid, as is declared.

**N**ow in few words to conclude, yee may by this Instru-  
ment measure the distalce of Houses, Steeples, Trees,  
the length of Walles, the breadth of Ditches, Images in  
height, and such like. The good wittie Carpenter standing  
in a place, where hee may plainly see a whole house, or any  
manner frame with great pleasure, may by this get speedily  
the true proportion of that house, whiche he ought to note in a  
Table, and whentime commeth (not without his great praise)  
may make reare and set by the like. This I take to be suffici-  
ent for these Craftsmen.

A more larger  
vse of this In-  
strument.

I haue

## The vle of the, &c.

How the  
length of land  
is exactly foud.

I haue before forgotten to admonish you whensoever ye list to measure any Land exactly, by the instrument Geometricall, named the Profitable Staffe, to set by right a Rodde, the length of a Pearch. Or if the distancke be long, to passe out, or rather iustly mete fwe or moe Pearches at the end or head of your length, the extremes noted with two visiblie marks. Then goe from thence, and seeke the length by that certayne widenesse, as is declared: so shall ye not faile to bring very true Land. Note that a little ercox found on the breadth, oft multiplied, encreaseth to a great, yea, to an intolerable fault in the length, wherefore the breadth or widenesse ought truly to be seachted. This I take sufficient for these Craftsmen.

I would desire where my grosse writings seeme to bee obscure, that I were present the instructer: for truly a lively booke of a meane speculator somewhat practised, furthereth tenne fold more in my iudgement, then the finest writer.

Farewell. Accept my good will, and looke shorly (if  
God spare life) for a profitable encrease  
of these matters.

FINIS.

